

HIAF 高能终端谱仪合作组会议, Nov 15-18, 2024



# HIAF能区超子-核子相互作用和超核产生研究

**Zhao-Qing Feng (冯兆庆)**

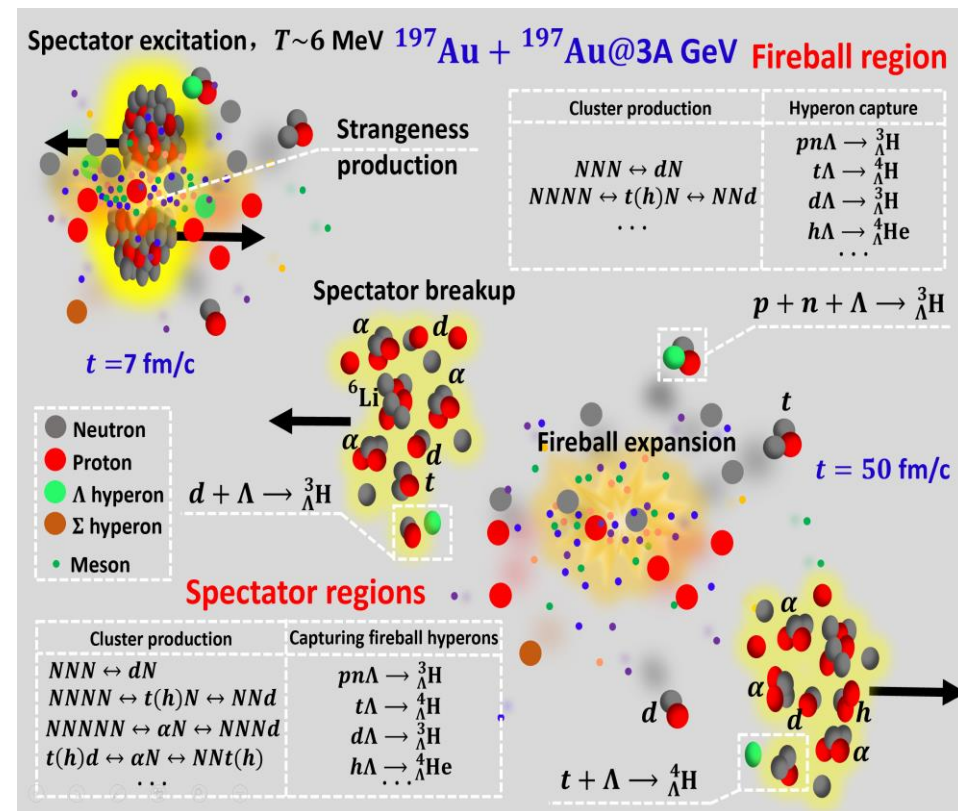
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# 报告概要

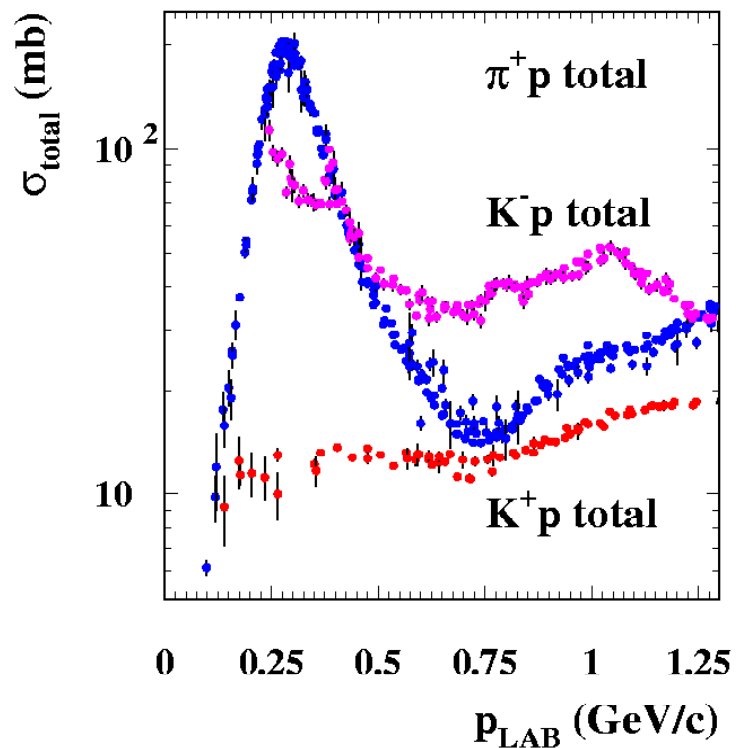
- 超子-核子相互作用和超核物理研究进展
- LQMD 运输模型
- 超子-核子相互作用和中子星物质性质
- 超核产生动力学研究
- HIAF 装置  $\pi$  介子和反质子束流相关物理讨论
- 总结和展望



# I. 超子-核子相互作用和超核物理研究进展



## 1. Strange particles production in hadron-hadron collisions

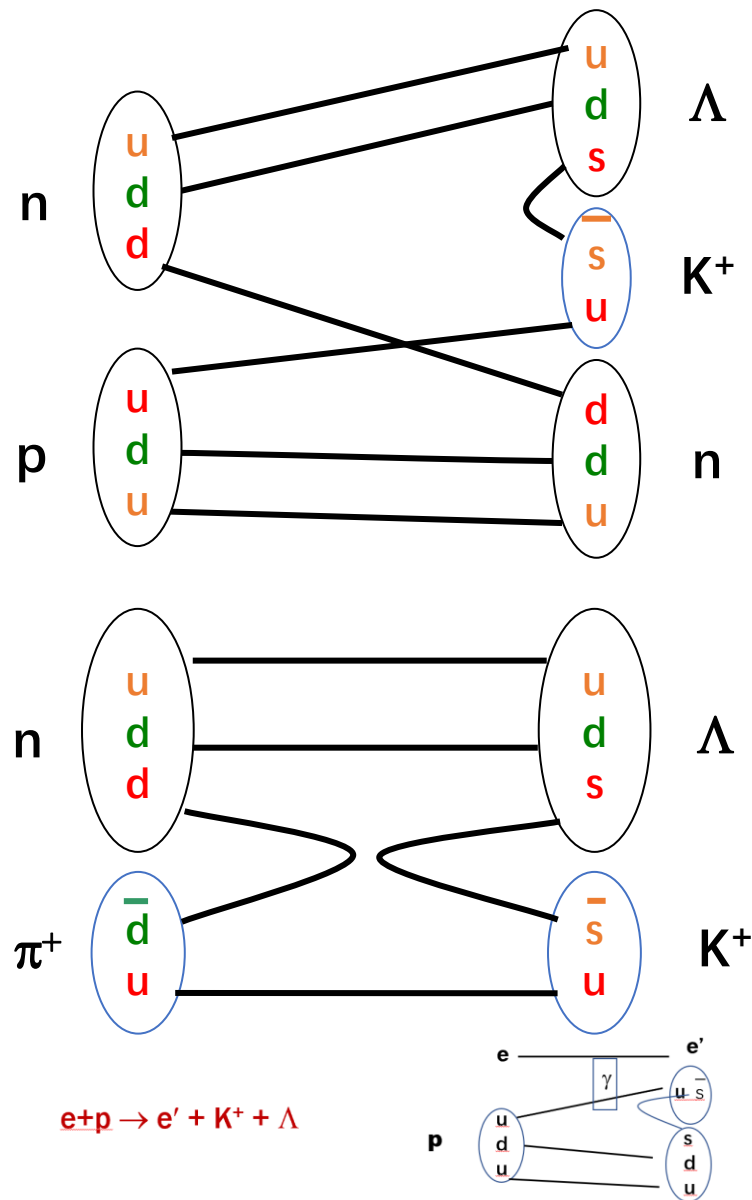


mean free path at  $\rho_0$ :

$$\lambda(\pi) = 0.3 \text{ fm}$$

$$\lambda(K^+) = 5 \text{ fm}$$

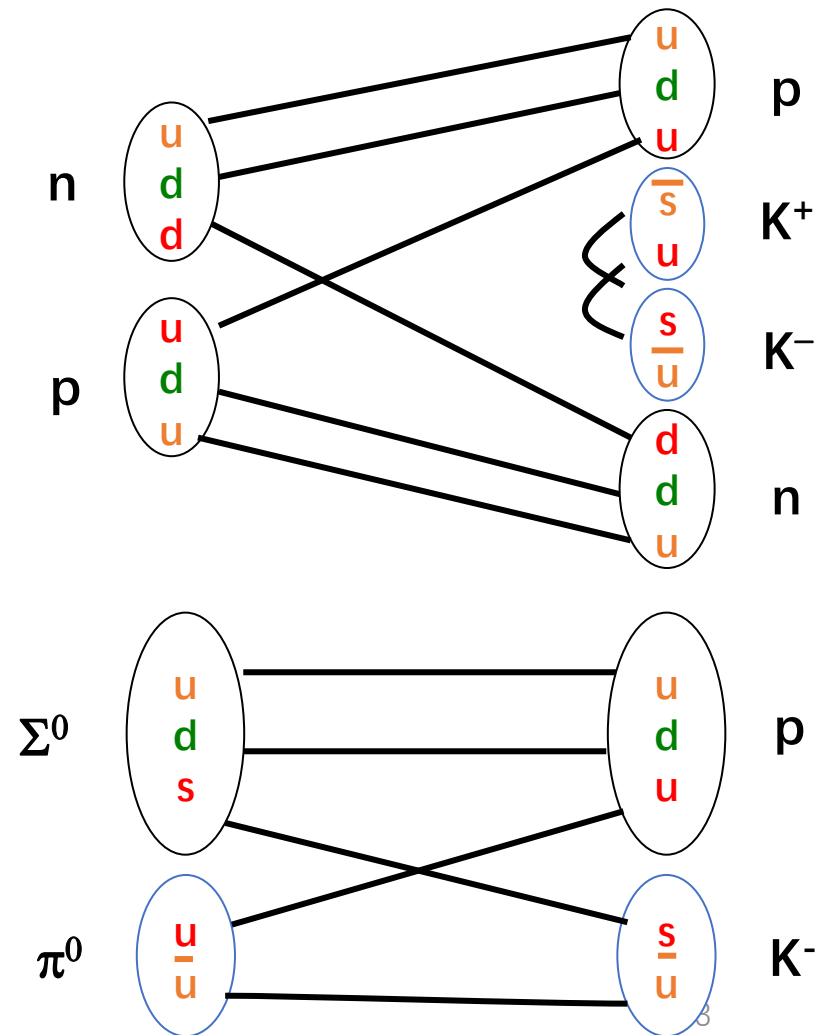
$$\lambda(K^-) = 0.8 \text{ fm}$$



科学通报 2018年 第63卷 第8期: 735-744

中高能重离子碰撞中奇异粒子产生和超核形成机制

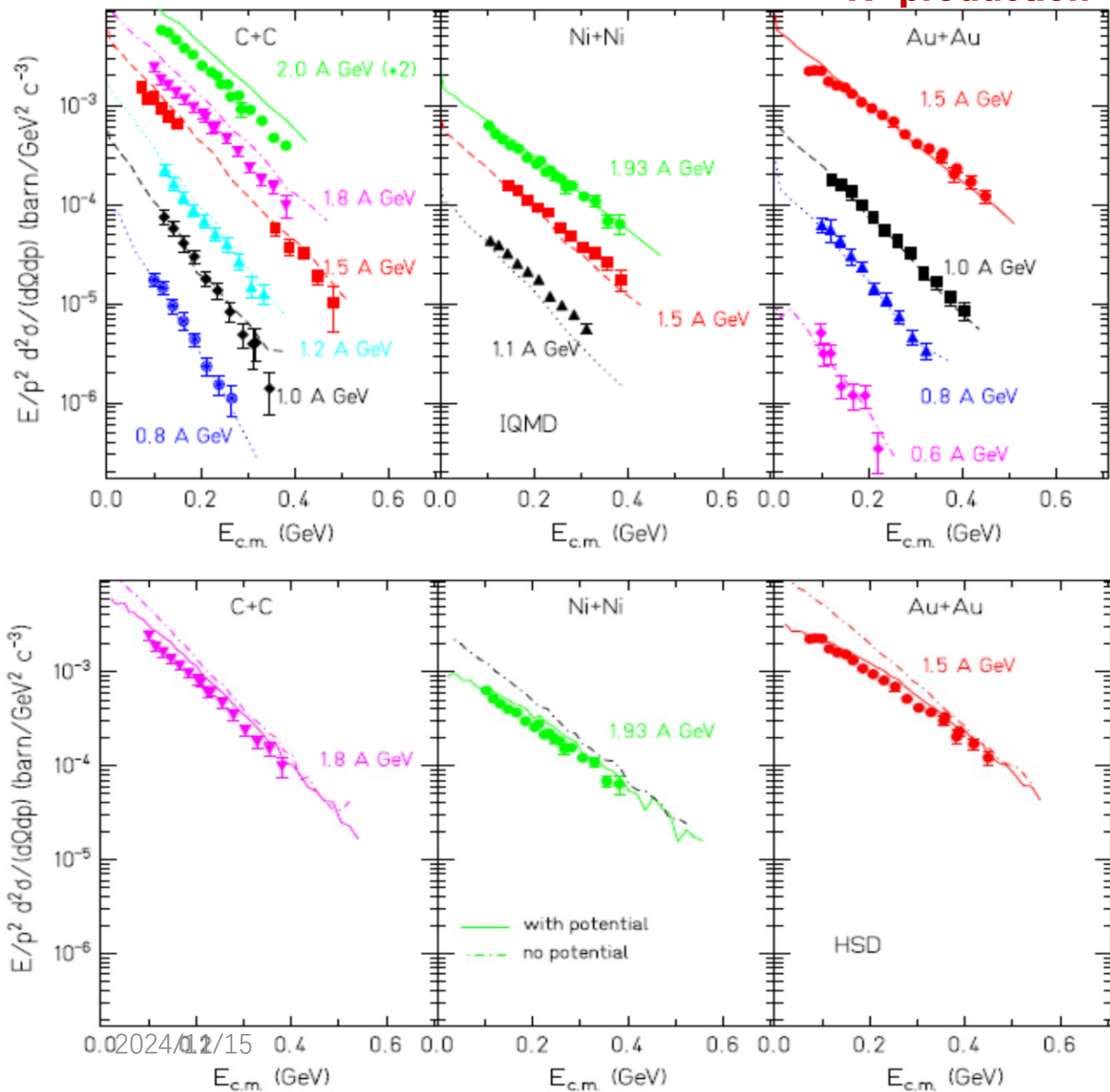
冯兆庆



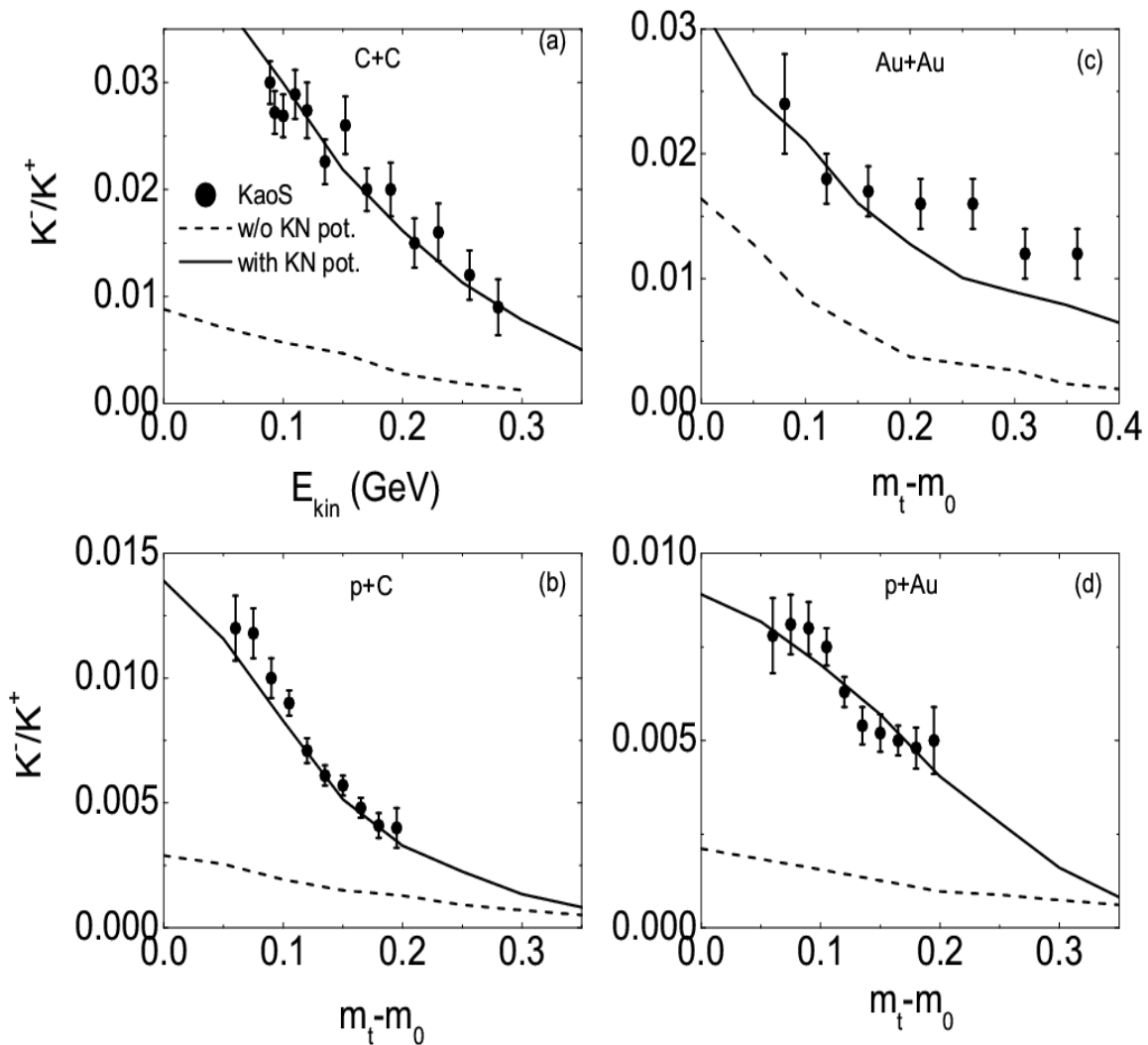
## 2. Strange particle production in HICs

C. Hartnack et al. / Physics Reports 510 (2012) 119–200

**K<sup>+</sup> production**



Z. Q. Feng et al., Phys. Rev. C 90, 064604 (2014)



$$V_{K^+}(\rho_0) = 28 \text{ MeV}, \quad V_{K^-}(\rho_0) = -100 \text{ MeV}$$

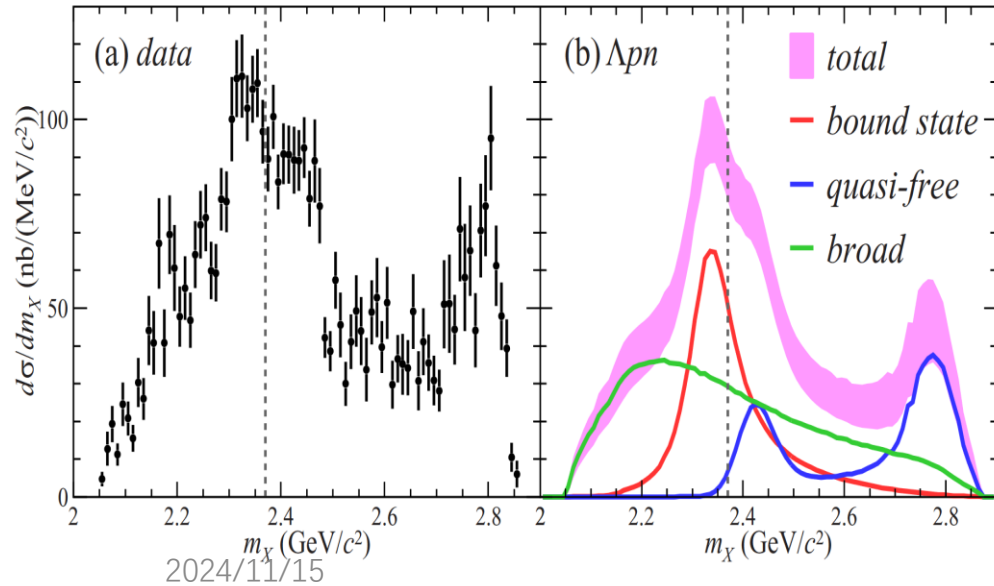


### 3. Hypernuclear production in HICs

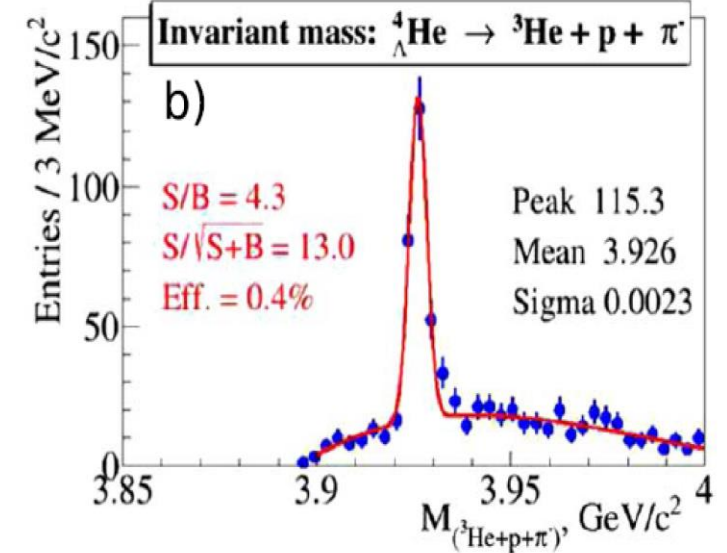
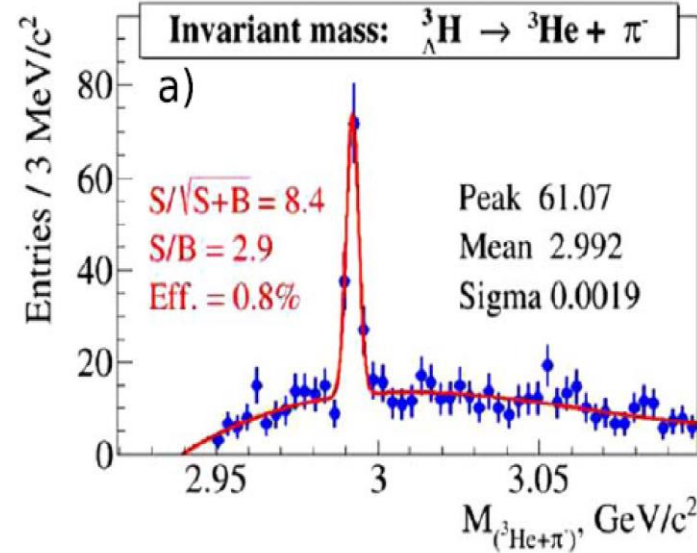
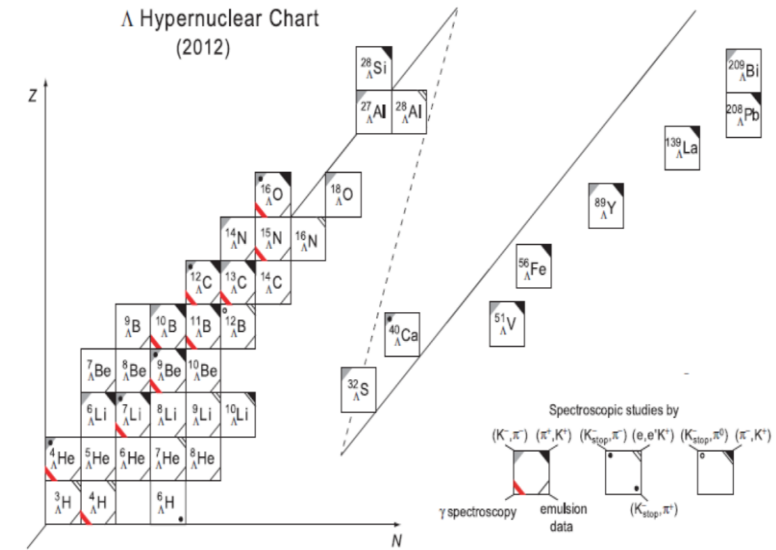
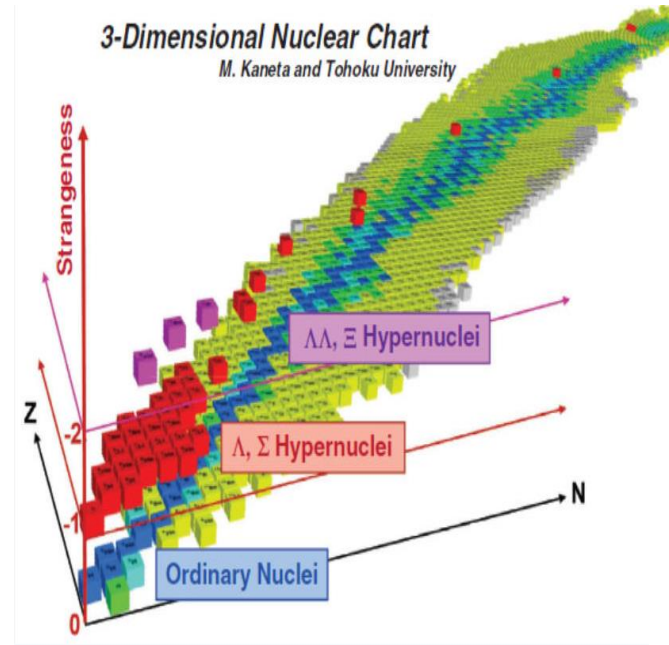
- ① Neutron-rich/proton-rich HN nuclei and spectroscopies
- ② Multistrangeness HN ( $S=-2$ )  $\Lambda\Lambda$ X and  $\Xi$ X
- ③ Interaction potentials of  $N\Lambda$ ,  $N\Xi$ ,  $NN\Lambda$ , etc

PHYSICAL REVIEW C **102**, 044002 (2020)

Observation of a  $\bar{K}NN$  bound state in the  ${}^3\text{He}(K^-, \Lambda p)n$  reaction



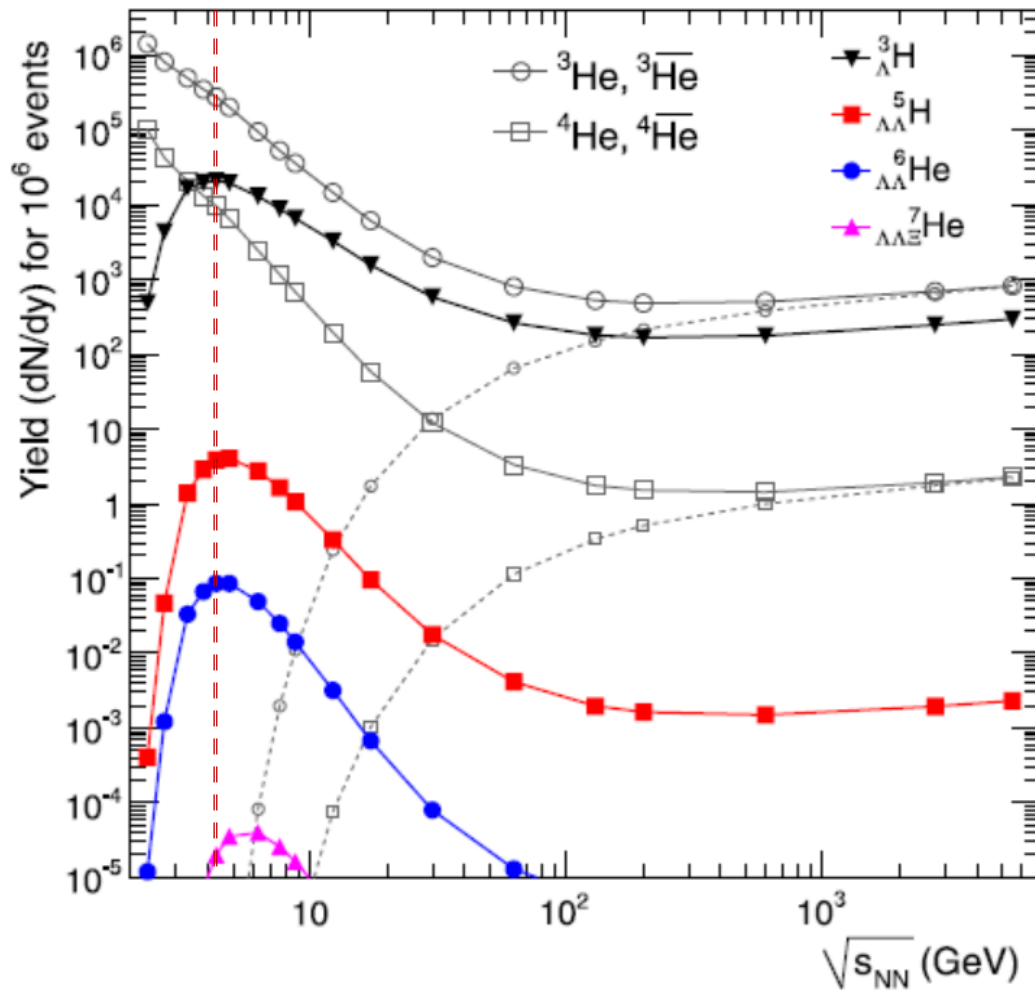
H. Tamura, *Prog. Theor. Exp. Phys.* (2012) 02B012



# (Hyper-)cluster production in HICs-statistical approach

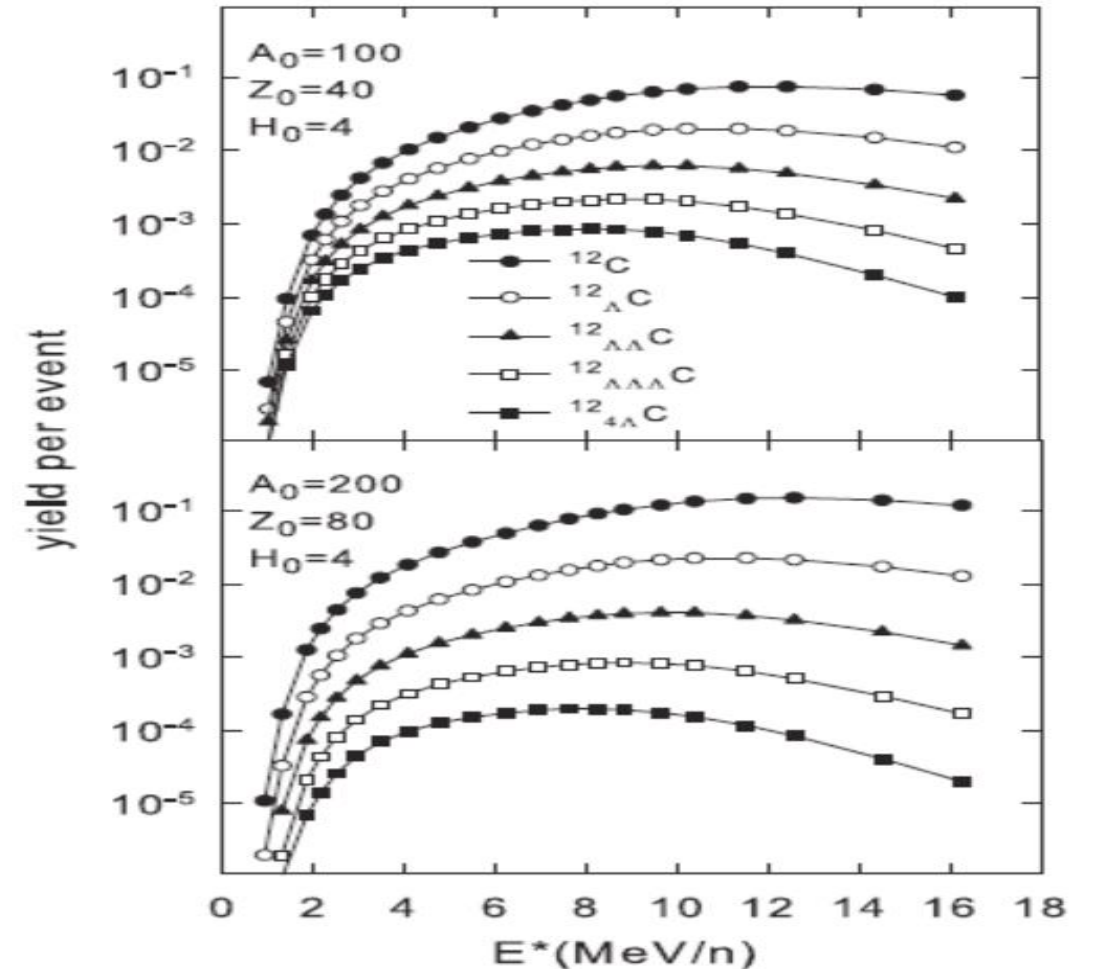
A. Andronic, P. Braun-Munzinger, J. Stachel, H. Stöcker,  
Physics Letters B 697 (2011) 203–207

Pb+Pb



N. Buyukcizmeci, R. Ogul, A. S. Botvina, M.  
Bleicher, Phys. Scr. 95 075311 (2020)

Statistical multifragmentation model (SMM)

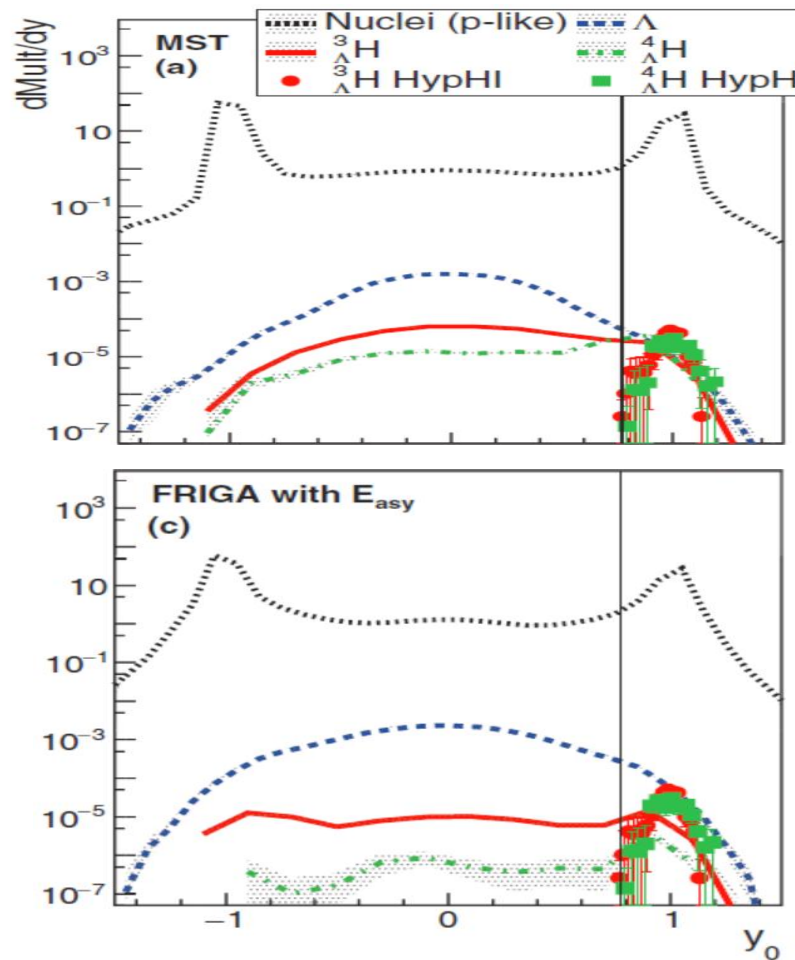
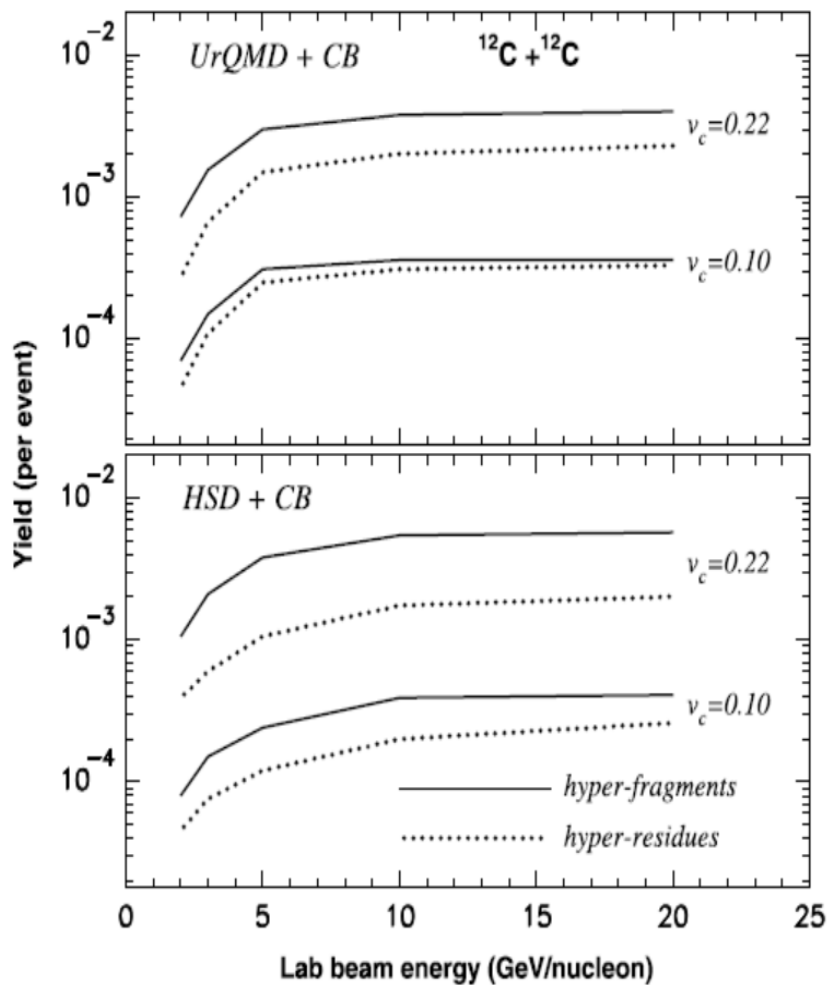


# Transport model + coalescence approach

A.S. Botvina, J. Steinheimer, E. Bratkovskaya et al., Physics Letters B 742 (2015) 7-14

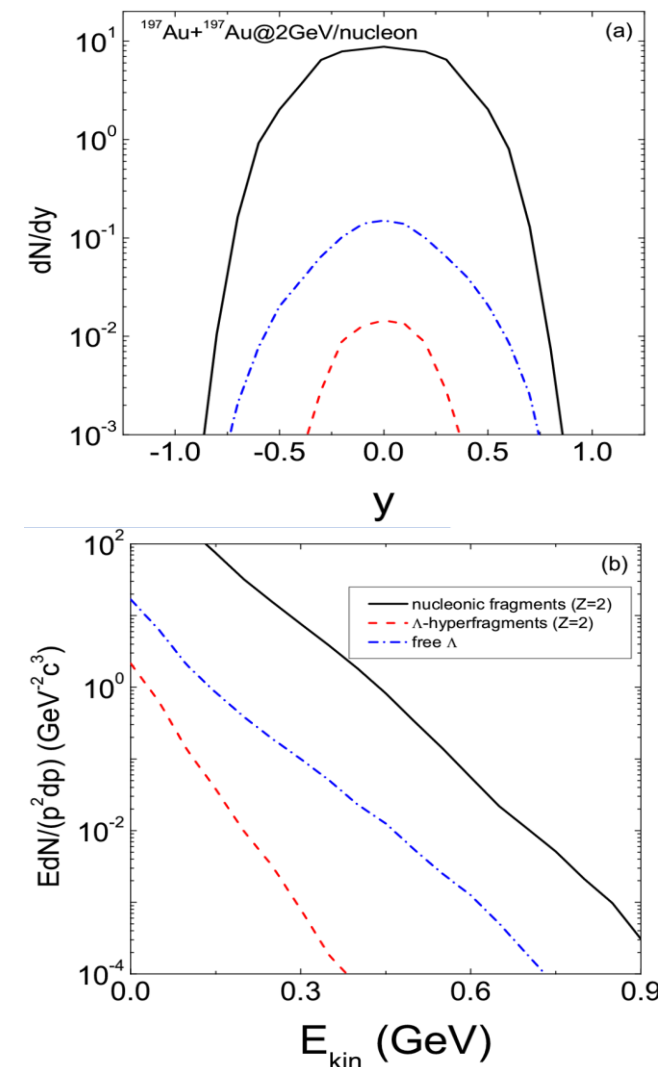
J. Aichelin, E. Bratkovskaya, A. Le Fèvre et al., Physical Review C 101, 044905 (2020)  
 A. Le Fèvre, J. Aichelin, C. Hartnack and Y. Leifels 100, Physical Review C 034904 (2019)

**${}^6\text{Li}+{}^{12}\text{C}@2\text{A GeV}$**



中高能重离子碰撞中奇异粒子产生和超核形成机制

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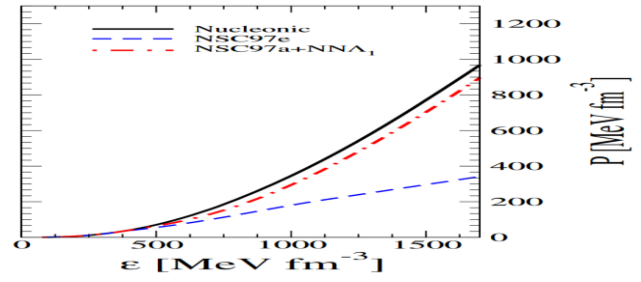
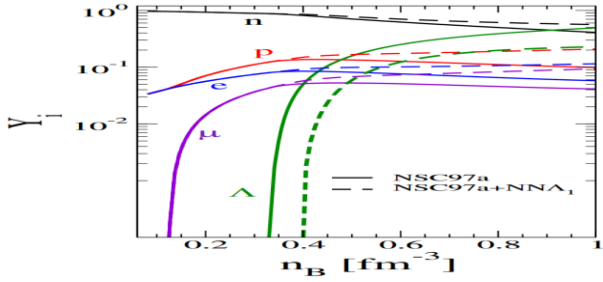
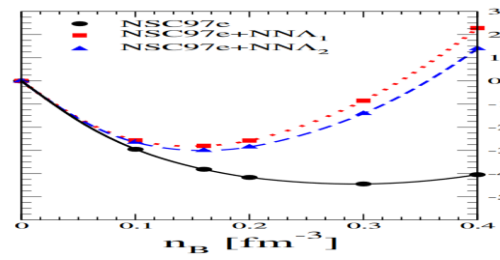
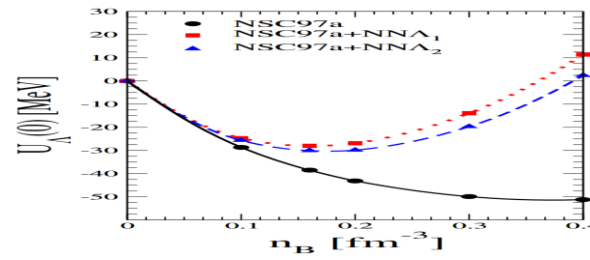
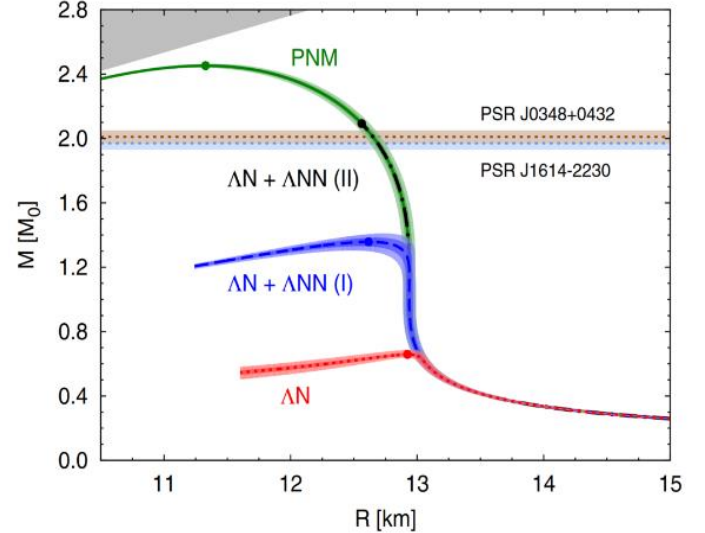
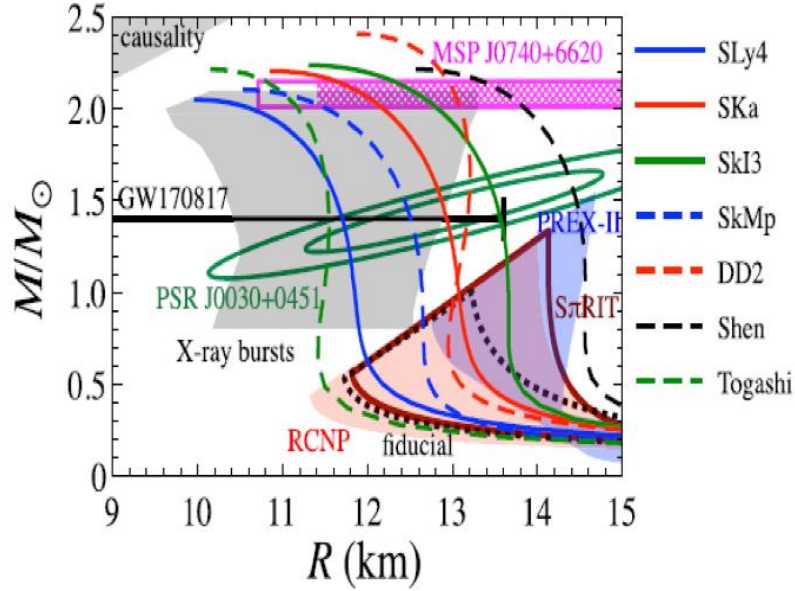
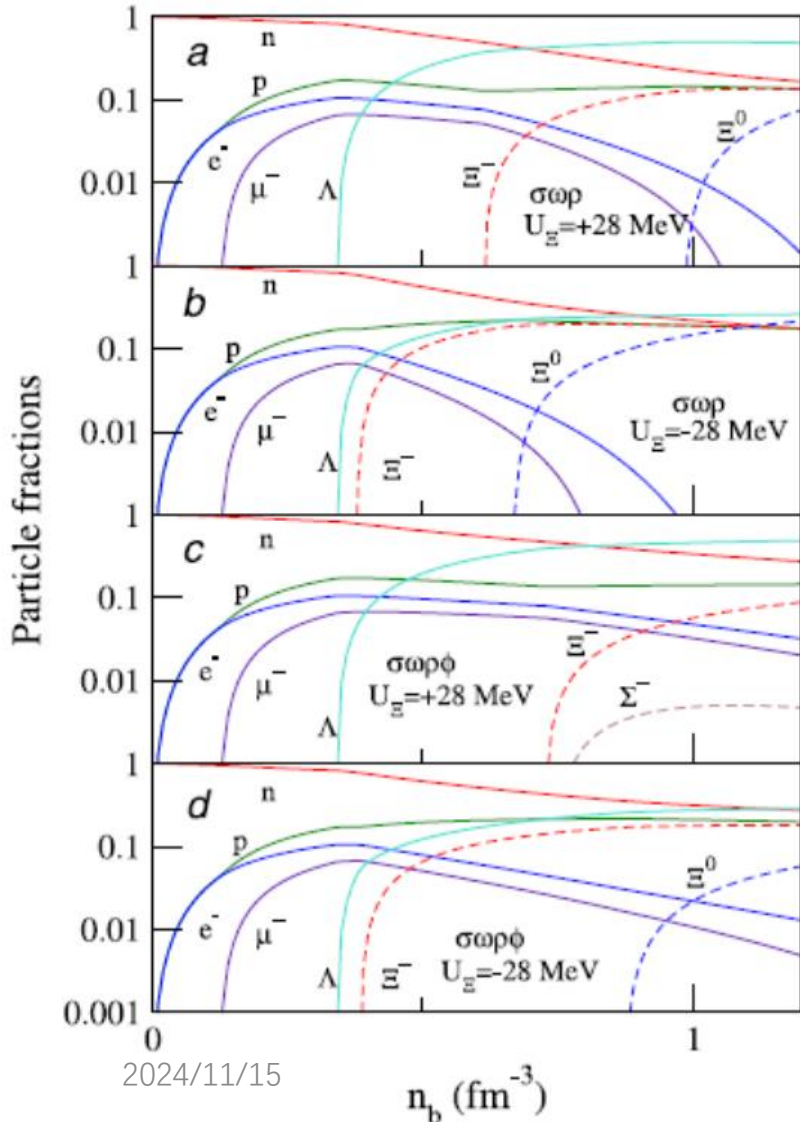


# Hyperons in neutron stars (NS)

S. Weissenborn, D. Chatterjee, J. Schaffner-Bielich, Nucl. Phys. A 881, 62 (2012)

W. Z. Jiang, R. Y. Yang, and D. R. Zhang, Phys. Rev. C 87, 064314 (2013)

Diego Lonardonì, Alessandro Lovato, Stefano Gandolfi, and Francesco Pederiva, Phys. Rev. Lett. 114, 092301 (2015)

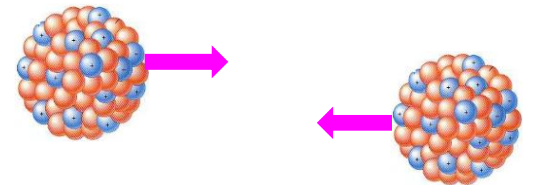




# Lanzhou quantum molecular dynamics transport model (LQMD)

Heavy-ion collisions (5 MeV – 5 GeV/nucleon) and hadron induced reaction ( $p$ ,  $\bar{p}$ ,  $\pi$ ,  $K$ ,  $e$ , etc)

- **LQMD transport model** (Skyrme interaction, Walecka model with  $\sigma$ ,  $\omega$ ,  $\rho$ ,  $\delta$ )
- **Neutron star equation of state** (nuclear **symmetry energy** at sub- and supra- saturation densities in HICs, isospin splitting of nucleon effective mass from HICs, particle production, 2-body and 3-body potential, multi-body correlation)
- **In-medium effects of hadrons** (optical potentials, energy conservation and in-medium effects, i.e.,  $\Delta(1232)$ ,  $N^*(1440)$ ,  $N^*(1535)$ ), hyperons ( $\Lambda, \Sigma, \Xi$ ) and mesons ( $\pi, K, \eta, \rho, \omega, \phi \dots$ )
- **Kinetic production of (hyper)clusters and nuclear fragmentation reactions** (production cross section, phase-space distribution, collective flows, cluster transportation, Mott effect, e.g., deuteron, triton,  $^3\text{He}$ ,  $\alpha$ ,  $_{\Lambda(\Sigma)}X$ ,  $_{\Lambda\Lambda}X$ ,  $_{\Xi}X$ ,  $_{\bar{\Lambda}}X$ )
- **Nuclear fusion near Coulomb barrier energies** (barrier distribution, neck dynamics, fusion cross section etc)
- **Hadron induced nuclear reactions** (spallation reaction, physics at PANDA such as hypernuclear, neutron skin thickness etc)



# 1. Lanzhou quantum molecular dynamics transport model (LQMD-Skyrme)

PHYSICAL REVIEW C 84, 024610 (2011)

Momentum dependence of the symmetry potential and its influence on nuclear reactions

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(Received 11 July 2011; published 19 August 2011)

$$H_B = \sum_i \sqrt{\mathbf{p}_i^2 + \mathbf{m}_i^2} + U_{\text{int}} + U_{\text{mom}}$$

$$U_{\text{loc}} = \int V_{\text{loc}}(\rho(\mathbf{r})) d\mathbf{r}$$

$$V_{\text{loc}}(\rho) = \frac{\alpha}{2} \frac{\rho^2}{\rho_0} + \frac{\beta}{1+\gamma} \frac{\rho^{1+\gamma}}{\rho_0^\gamma} + E_{\text{sym}}^{\text{loc}}(\rho) \rho \delta^2 + \frac{g_{\text{sur}}}{2\rho_0} (\nabla \rho)^2 + \frac{g_{\text{sur}}^{\text{iso}}}{2\rho_0} [\nabla(\rho_n - \rho_p)]^2,$$

Phys. Rev. C 84, 024610  
(2011); 85, 014604 (2012)

$$U_{\text{mom}} = \frac{1}{2\rho_0} \sum_{i,j,j \neq i} \sum_{\tau,\tau'} C_{\tau,\tau'} \delta_{\tau,\tau_i} \delta_{\tau',\tau_j} \iiint d\mathbf{p} d\mathbf{p}' d\mathbf{r} f_i(\mathbf{r}, \mathbf{p}, t) \times [\ln(\epsilon(\mathbf{p} - \mathbf{p}')^2 + 1)]^2 f_j(\mathbf{r}, \mathbf{p}', t).$$

$$E_{\text{sym}}(\rho) = \frac{1}{3} \frac{\hbar^2}{2m} \left( \frac{3}{2} \pi^2 \rho \right)^{2/3} + E_{\text{sym}}^{\text{loc}}(\rho) + E_{\text{sym}}^{\text{mom}}(\rho).$$

$$C_{\text{sym}} = 38 \text{ MeV}$$

$$a_{\text{sym}} = 37.7 \text{ MeV}$$

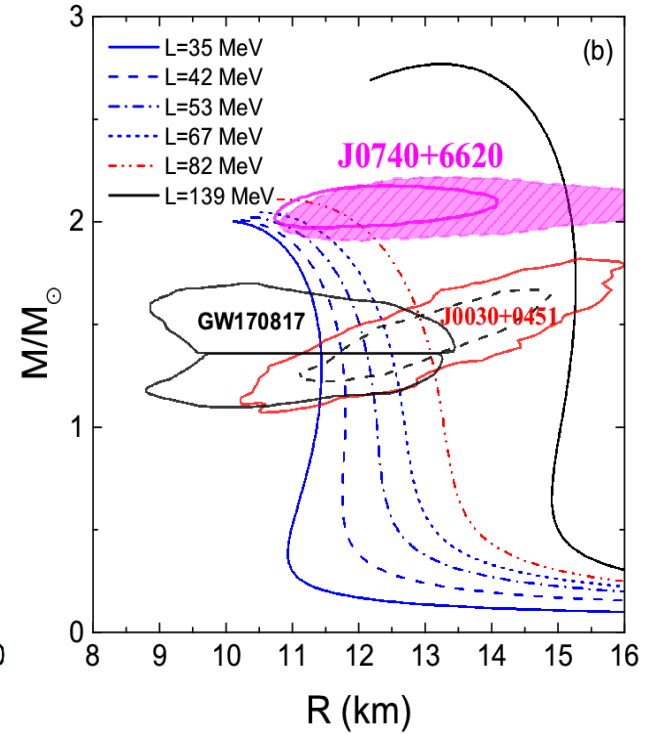
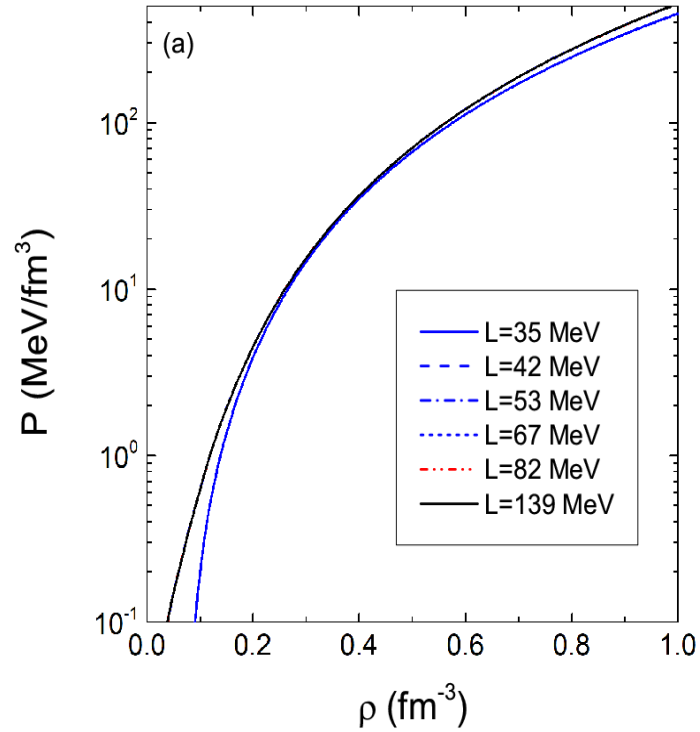
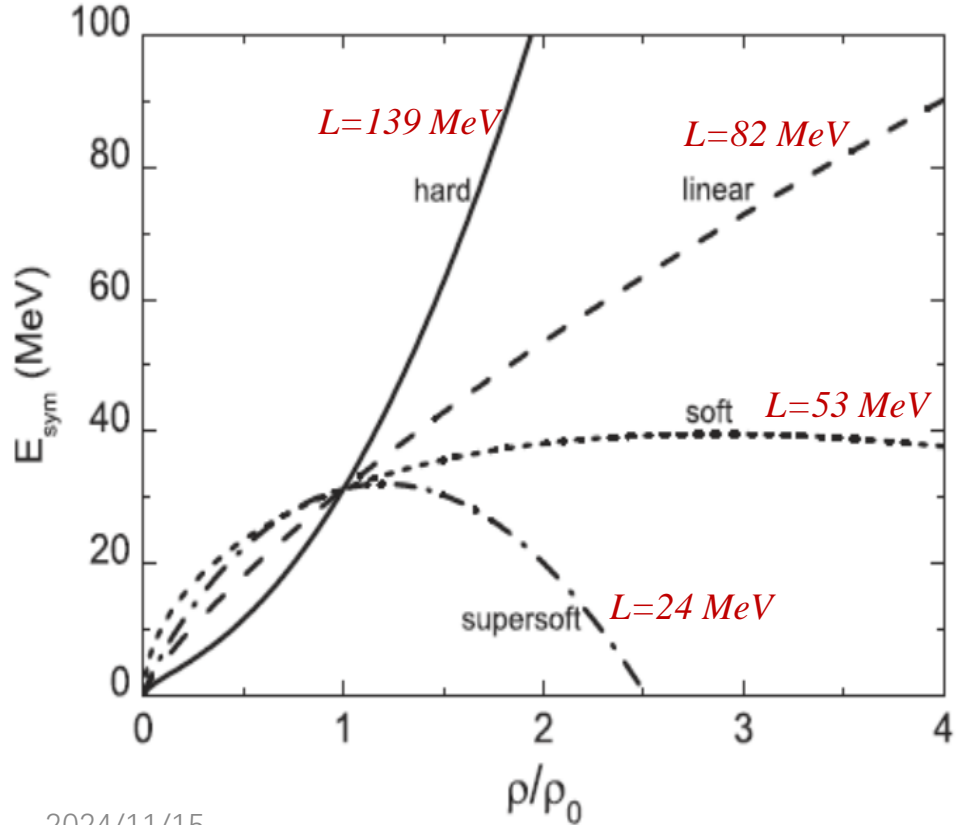
$$b_{\text{sym}} = -18.7 \text{ MeV}$$

$$E_{\text{sym}}^{\text{loc}}(\rho) = \frac{1}{2} C_{\text{sym}} (\rho / \rho_0)^{\gamma_s}$$

$$E_{\text{sym}}^{\text{loc}}(\rho) = a_{\text{sym}} (\rho / \rho_0) + b_{\text{sym}} (\rho / \rho_0)^2.$$

Table 1: The parameters and properties of isospin symmetric EoS used in the LQMD model at the density of  $0.16 \text{ fm}^{-3}$ .

Parameters	$\alpha$ (MeV)	$\beta$ (MeV)	$\gamma$	$C_{mom}$ (MeV)	$\epsilon$ ( $c^2/\text{MeV}^2$ )	$m_\infty^*/m$	$K_\infty$ (MeV)
PAR1	-215.7	142.4	1.322	1.76	$5 \times 10^{-4}$	0.75	230
PAR2	-226.5	173.7	1.309	0.	0.	1.	230



## 2. Covariant energy-density functional (LQMD.RMF)

Si-Na Wei, Zhao-Qing Feng,  
Nuclear Science and Techniques 35, 15 (2024)  
arXiv:2302.09984

$$L = \bar{\psi}[i\gamma_\mu \partial^\mu - (M_N - g_\sigma \varphi - g_\delta \vec{\tau} \cdot \vec{\delta}) - g_\omega \gamma_\mu \omega^\mu - g_\rho \gamma_\mu \vec{\tau} \cdot \vec{b}^\mu] \psi \\ + \frac{1}{2} (\partial_\mu \varphi \partial^\mu \varphi - m_\sigma^2 \varphi^2) - U(\varphi) + \frac{1}{2} (\partial_\mu \vec{\delta} \partial^\mu \vec{\delta} - m_\delta^2 \vec{\delta}^2) \\ + \frac{1}{2} m_\omega^2 \omega_\mu \omega^\mu - \frac{1}{4} F_{\mu\nu} F^{\mu\nu} + \frac{1}{2} m_\rho^2 \vec{b}_\mu \vec{b}^\mu - \frac{1}{4} \vec{G}_{\mu\nu} \vec{G}^{\mu\nu}$$

$$F_{\mu\nu} = \partial_\mu \omega_\nu - \partial_\nu \omega_\mu, \\ G_{\mu\nu} = \partial_\mu \vec{b}_\nu - \partial_\nu \vec{b}_\mu, \\ U(\varphi) = \frac{g_2}{3} \varphi^3 + \frac{g_3}{4} \varphi^4$$

### Energy density functional

$$\varepsilon = \sum_{i=n,p} 2 \int \frac{d^3k}{(2\pi)^3} \sqrt{k^2 + M_i^{*2}} + \frac{1}{2} m_\sigma^2 \varphi^2 + U(\varphi) + \frac{1}{2} m_\omega^2 \omega_0^2 + \frac{1}{2} m_\rho^2 b_0^2 + \frac{1}{2} m_\delta^2 \delta_3^2$$

### Temporal evolution in phase space

$$\dot{\mathbf{x}} = \frac{\mathbf{p}_i^*}{p_0^*} + \sum_{i \neq j}^N \left\{ \frac{g_v^2}{2m_v^2} z_j^{*\mu} u_{i,\mu} B_i B_j \frac{\partial \rho_{ij}}{\partial \mathbf{p}_i} + \frac{g_v^2}{2m_v^2} z_i^{*\mu} u_{j,\mu} B_i B_j \frac{\partial \rho_{ji}}{\partial \mathbf{p}_i} + \frac{g_v^2}{2m_v^2} z_j^{*\mu} \rho_{ji} B_i B_j \frac{\partial u_{i,\mu}}{\partial \mathbf{p}_i} \right. \\ \left. + z_j^{*\mu} \frac{B_i B_j \bar{g}_v^2}{2m_v^2} \left[ \frac{\rho_{ij}}{1 - p_{T,ij}^2/\Lambda_v^2} \frac{\partial u_{i,\mu}}{\partial \mathbf{p}_i} + \frac{u_{i,\mu}}{1 - p_{T,ij}^2/\Lambda_v^2} \frac{\partial \rho_{ij}}{\partial \mathbf{p}_i} + u_{i,\mu} \rho_{ij} \frac{\partial [1/(1 - p_{T,ij}^2/\Lambda_v^2)]}{\partial \mathbf{p}_i} \right] \right. \\ \left. + z_i^{*\mu} \frac{B_i B_j \bar{g}_v^2}{2m_v^2} \left[ \frac{u_{j,\mu}}{1 - p_{T,ji}^2/\Lambda_v^2} \frac{\partial \rho_{ji}}{\partial \mathbf{p}_i} + u_{j,\mu} \rho_{ji} \frac{\partial [1/(1 - p_{T,ji}^2/\Lambda_v^2)]}{\partial \mathbf{p}_i} \right] \right. \\ \left. - \frac{m_j^*}{p_j^{*0}} \frac{\partial S_j}{\partial \mathbf{p}_i} - \frac{m_i^*}{p_i^{*0}} \frac{\partial S_i}{\partial \mathbf{p}_i} \right\}, \\ \dot{\mathbf{p}} = - \sum_{i \neq j}^N \left\{ \frac{g_v^2}{2m_v^2} z_j^{*\mu} u_{i,\mu} B_i B_j \frac{\partial \rho_{ij}}{\partial \mathbf{r}_i} + \frac{g_v^2}{2m_v^2} z_i^{*\mu} u_{j,\mu} B_i B_j \frac{\partial \rho_{ji}}{\partial \mathbf{r}_i} \right. \\ \left. + z_j^{*\mu} \frac{B_i B_j \bar{g}_v^2}{2m_v^2} \frac{u_{i,\mu}}{1 - p_{T,ij}^2/\Lambda_v^2} \frac{\partial \rho_{ij}}{\partial \mathbf{r}_i} \right. \\ \left. + z_i^{*\mu} \frac{B_i B_j \bar{g}_v^2}{2m_v^2} \frac{u_{j,\mu}}{1 - p_{T,ji}^2/\Lambda_v^2} \frac{\partial \rho_{ji}}{\partial \mathbf{r}_i} \right. \\ \left. - \frac{m_j^*}{p_j^{*0}} \frac{\partial S_j}{\partial \mathbf{r}_i} - \frac{m_i^*}{p_i^{*0}} \frac{\partial S_i}{\partial \mathbf{r}_i} \right\},$$

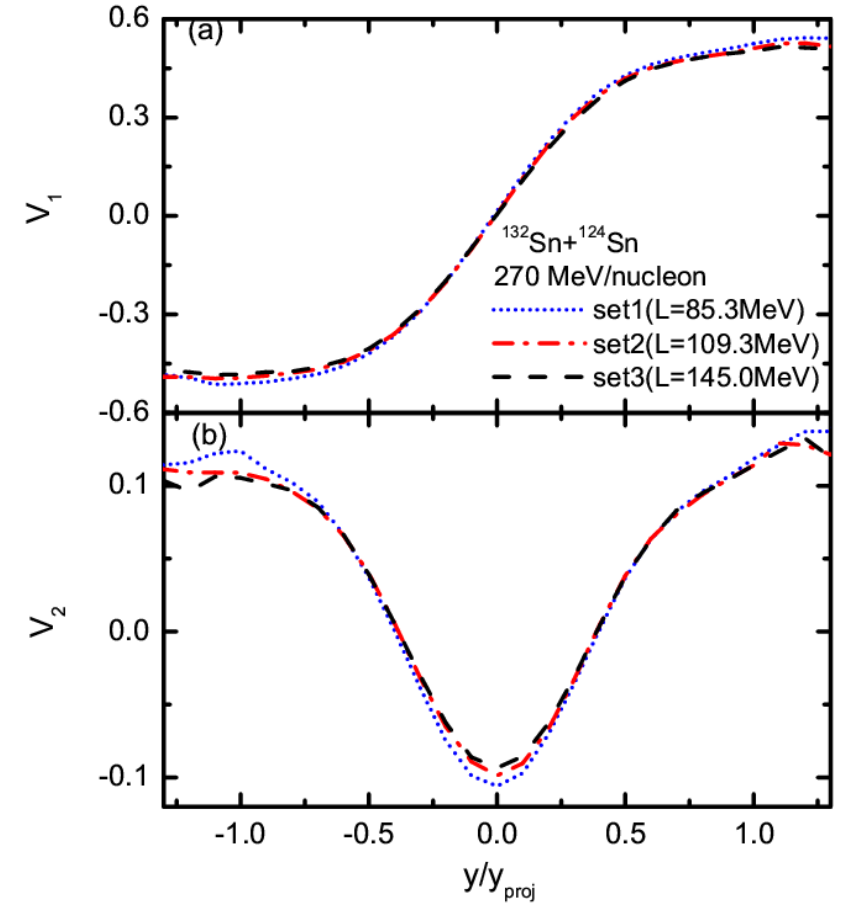
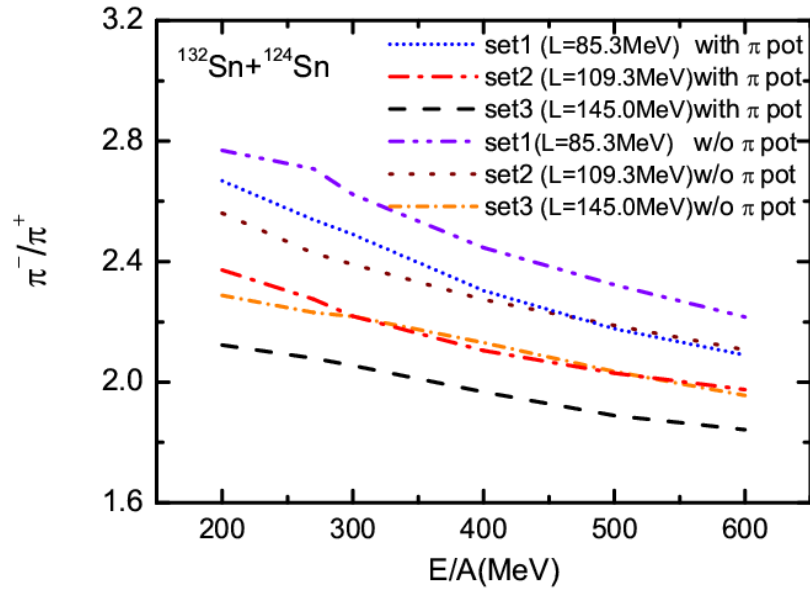
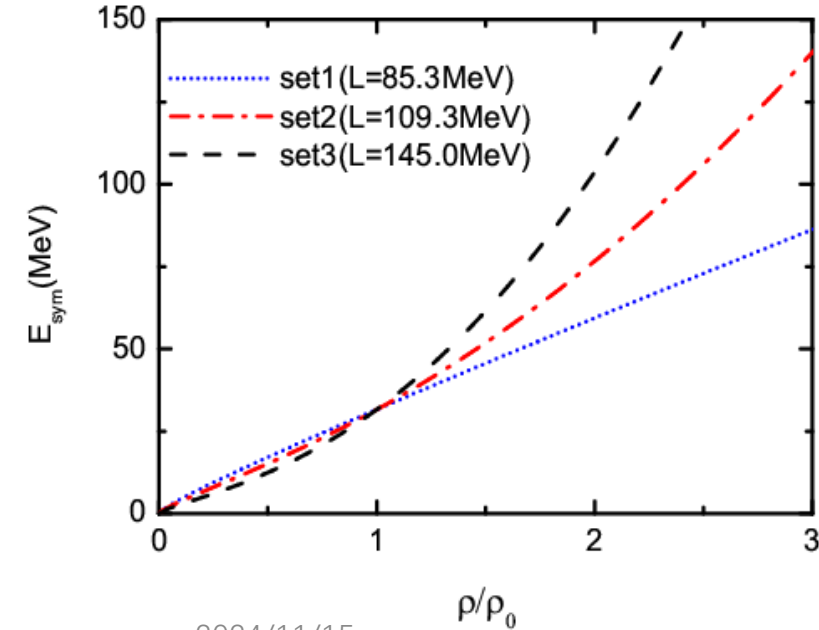


TABLE I: Parameter sets for RMF. The saturation density  $\rho_0$  is set to be  $0.16 \text{ fm}^{-3}$ . The binding energy of saturation density is  $E/A - M_N = -16 \text{ MeV}$ . The isoscalar-vector  $\omega$  and isovector-vector  $\rho$  masses are fixed to their physical values,  $m_\omega = 783 \text{ MeV}$  and  $m_\rho = 763 \text{ MeV}$ . The remaining meson mass  $m_\sigma$  is set to be  $550 \text{ MeV}$ .

model	$g_\sigma$	$g_\omega$	$g_2 \text{ (fm}^{-1}\text{)}$	$g_3$	$g_\rho$	$g_\delta$	$K \text{ (MeV)}$	$E_{sym}(\rho_0) \text{ (MeV)}$	$L(\rho_0) \text{ (MeV)}$
set1	8.145	7.570	31.820	28.100	4.049	-	230	31.6	85.3
set2	8.145	7.570	31.820	28.100	8.673	5.347	230	31.6	109.3
set3	8.145	7.570	31.820	28.100	11.768	7.752	230	31.6	145.0

**Symmetry energy** 
$$E_{sym} = \frac{1}{6} \frac{k_F^2}{E_F^*} + \frac{1}{2} \left[ f_\rho - f_\delta \left( \frac{M^*}{E_F^*} \right) \right] \rho$$

$$f_{\rho,\delta} = g_{\rho,\delta} / m_{\rho,\delta}$$



### 3. Particle production

$\pi$  and resonances ( $\Delta(1232)$ ,  $N^*(1440)$ ,  $N^*(1535)$ , ...) production:

$$\begin{aligned}
 NN &\leftrightarrow N\Delta, & NN &\leftrightarrow NN^*, & NN &\leftrightarrow \Delta\Delta, & \Delta &\leftrightarrow N\pi, \\
 N^* &\leftrightarrow N\pi, & NN &\leftrightarrow NN\pi(s\text{-state}), & N^*(1535) &\leftrightarrow N\eta
 \end{aligned}$$

Collisions between resonances,  $NN^* \leftrightarrow N\Delta$ ,  $NN^* \leftrightarrow NN^*$

Strangeness channels:

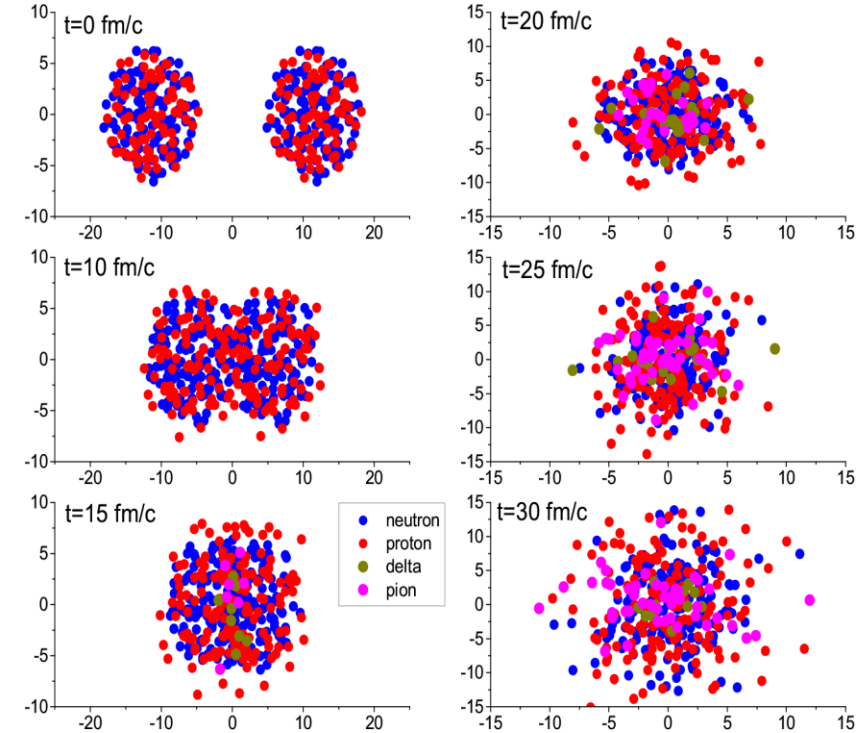
$$\begin{aligned}
 BB &\rightarrow BYK, & BB &\rightarrow BBK\bar{K}, & B\pi(\eta) &\rightarrow YK, & YK &\rightarrow B\pi, \\
 B\pi &\rightarrow NK\bar{K}, & Y\pi &\rightarrow B\bar{K}, & B\bar{K} &\rightarrow Y\pi, & YN &\rightarrow \bar{K}NN, \\
 BB &\rightarrow B\Xi KK, & \bar{K}B &\leftrightarrow K\Xi, & YY &\leftrightarrow N\Xi, & \bar{K}Y &\leftrightarrow \pi\Xi.
 \end{aligned}$$

Reaction channels with antiproton:

$$\bar{p}N \rightarrow \bar{N}N, \quad \bar{N}N \rightarrow \bar{N}N, \quad \bar{N}N \rightarrow \bar{B}B, \quad \bar{N}N \rightarrow \bar{Y}Y$$

$$\bar{N}N \rightarrow \text{annihilation}(\pi, \eta, \rho, \omega, K, \bar{K}, K^*, \bar{K}^*, \phi)$$

The **PYTHIA** and **FRITIOF** code are used for baryon(meson)-baryon and antibaryon-baryon collisions at high invariant energies



Statistical model with SU(3)

symmetry for annihilation

(E.S. Golubeva et al., Nucl. Phys. A 537, 393 (1992))

# III. 超子-核子相互作用和中子星物质性质

$$H_Y = \sum_{i=1}^{N_Y} V_i^{Coul} + V_{opt}^Y(\mathbf{p}_i, \rho_i) + \sqrt{\mathbf{p}_i^2 + m_Y^2}$$

$$V_{opt}^Y(\mathbf{p}_i, \rho_i) = \omega_Y(\mathbf{p}_i, \rho_i) - \sqrt{\mathbf{p}_i^2 + m_Y^2}$$

$$\omega_Y(\mathbf{p}_i, \rho_i) = \sqrt{(m_Y + \Sigma_S^Y)^2 + \mathbf{p}_i^2} + \Sigma_V^Y,$$

Phenomenological potential by fitting the results of chiral effective field theory

$$V_{opt}^\Lambda(\mathbf{p}_i, \rho_i) = V_a(\rho_i/\rho_0) + V_b(\rho_i/\rho_0)^2 + C_{mom}(\rho_i/\rho_0) \ln(\epsilon \mathbf{p}_i^2 + 1)$$

$$V_{opt}^\Sigma(\mathbf{p}_i, \rho_i) = V_0(\rho_i/\rho_0)^{\gamma_s} + V_1(\rho_n - \rho_p) t_\Sigma \rho_i^{\gamma_s} + C_{mom}(\rho_i/\rho_0) \ln(\epsilon \mathbf{p}_i^2 + 1).$$

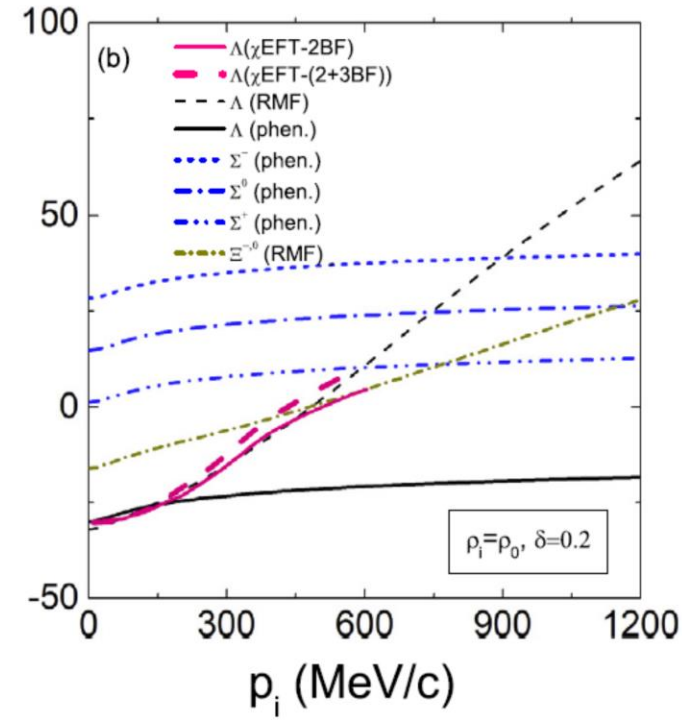
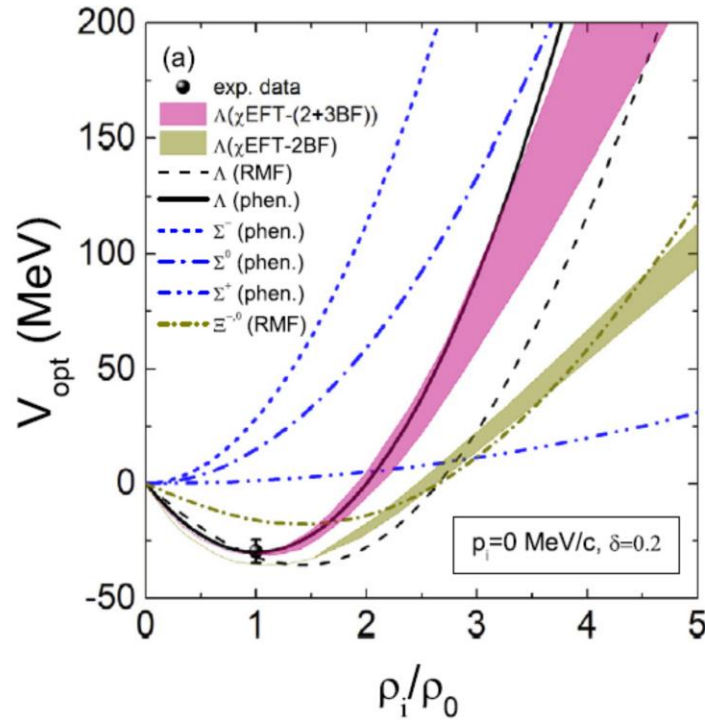


Letter

Extracting the hyperon-nucleon interaction via collective flows in heavy-ion collisions

Zhao-Qing Feng <sup>ORCID</sup>

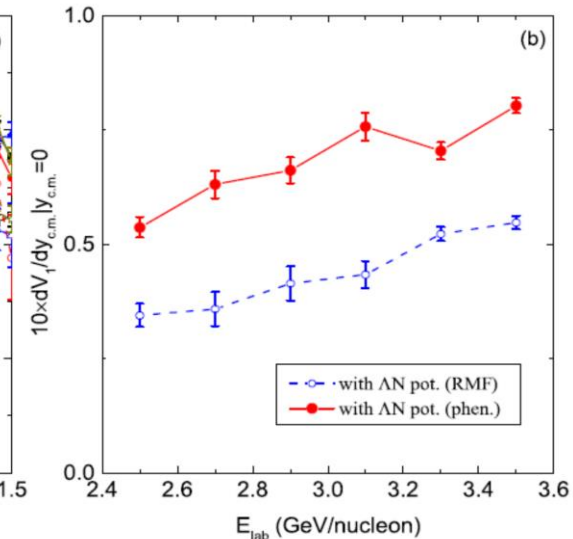
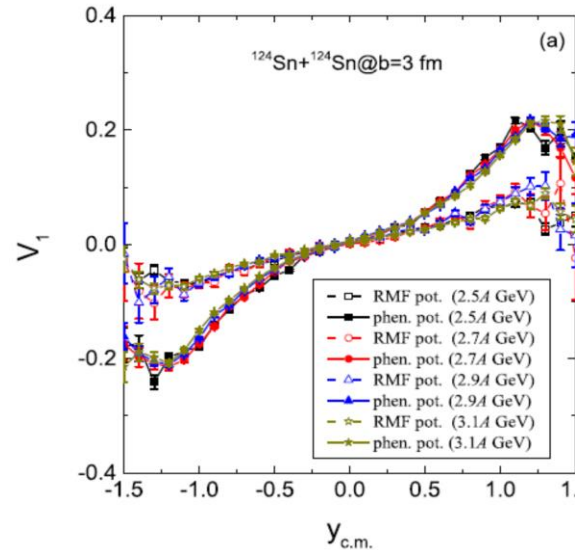
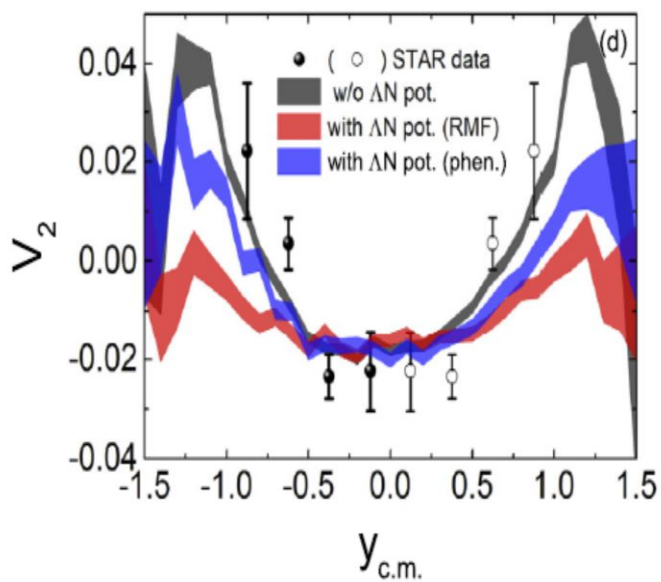
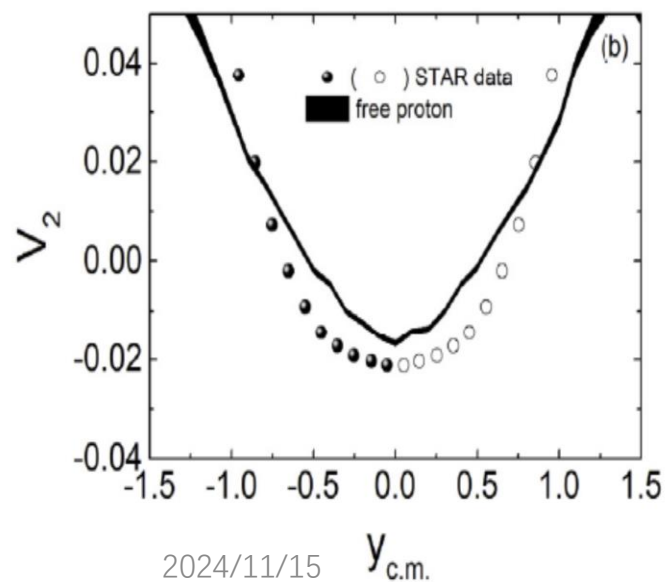
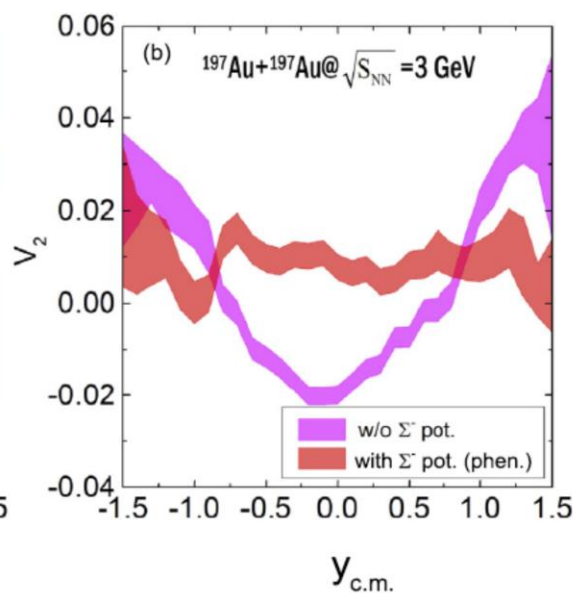
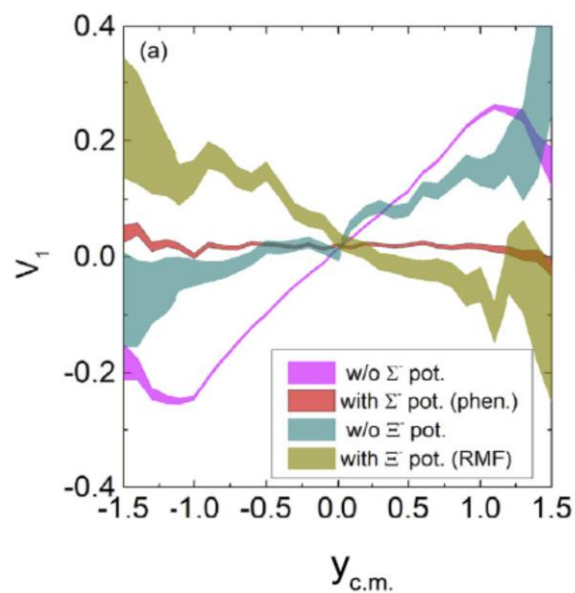
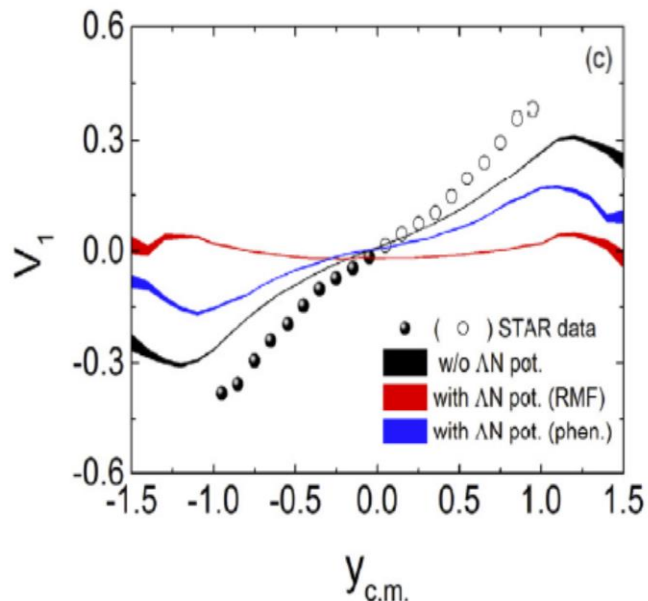
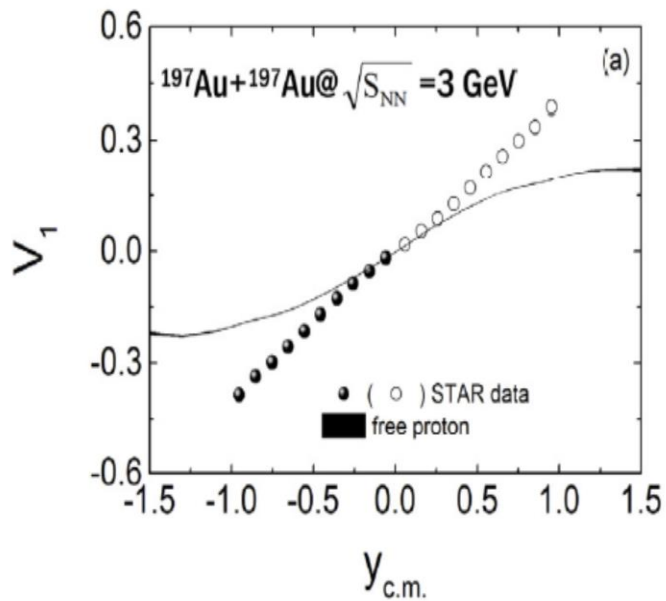
School of Physics and Optoelectronics, South China University of Technology, Guangzhou 510640, China





# Extracting the hyperon-nucleon interaction via collective flows in heavy-ion collisions

Phys. Lett. B 851 (2024) 138580





# The general flavor SU(3) symmetry

$$\mathcal{L}_{int} = \sum_B \bar{\Psi}_B [g_{B\sigma}\sigma - \gamma_\mu (g_{B\omega}\omega^\mu + g_{B\phi}\phi^\mu + g_{B\rho}\vec{\tau} \cdot \vec{b}^\mu)$$

$$] \Psi_B - \frac{1}{3} g_2 \sigma^3 - \frac{1}{4} g_3 \sigma^4,$$

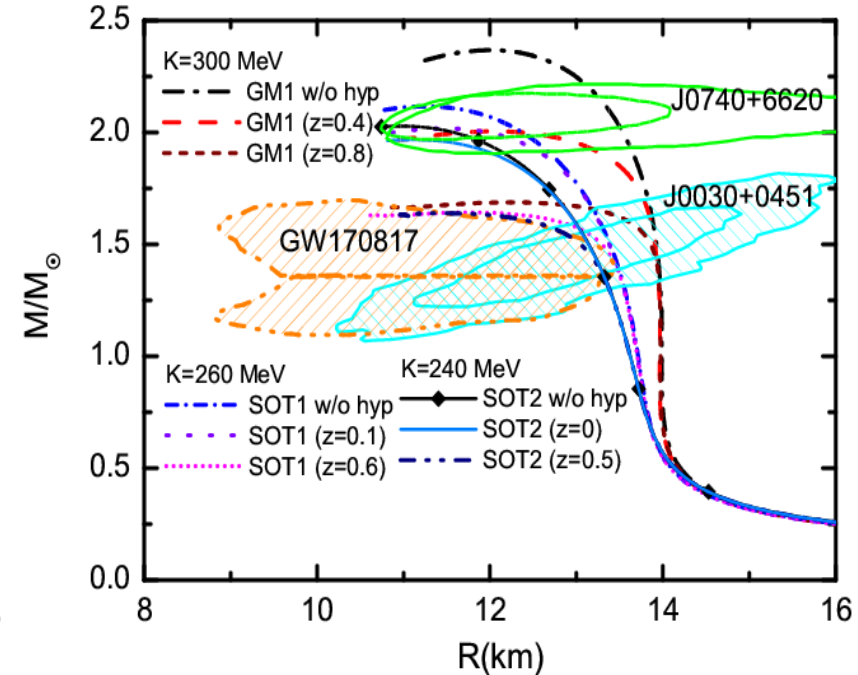
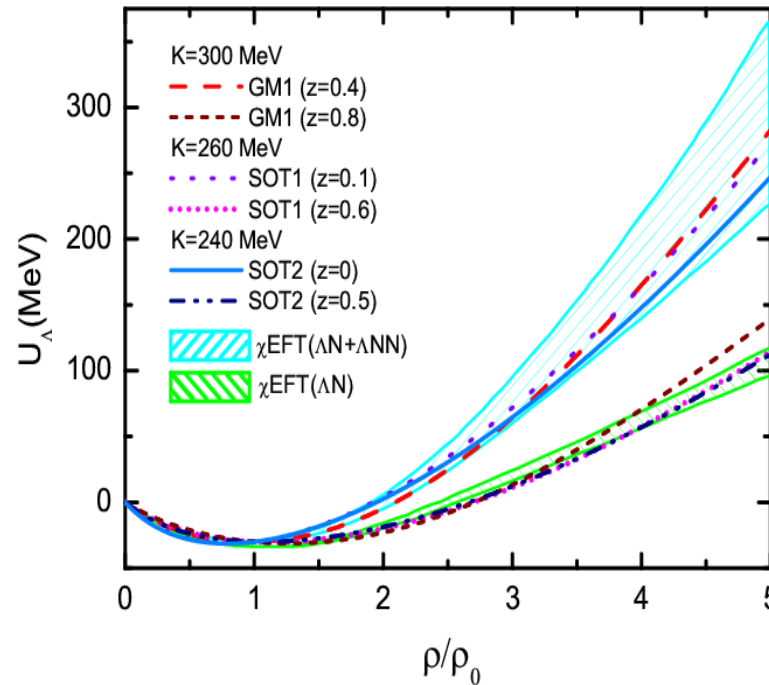
$$\frac{g_{\Lambda\omega}}{g_{N\omega}} = \frac{g_{\Sigma\omega}}{g_{N\omega}} = \frac{\sqrt{2}}{\sqrt{2} + \sqrt{3}z},$$

$$\frac{g_{\Lambda\phi}}{g_{N\omega}} = \frac{g_{\Sigma\phi}}{g_{N\omega}} = \frac{-1}{\sqrt{2} + \sqrt{3}z},$$

$$\frac{g_{\Xi\omega}}{g_{N\omega}} = \frac{\sqrt{2} - \sqrt{3}z}{\sqrt{2} + \sqrt{3}z},$$

$$\frac{g_{\Xi\phi}}{g_{N\omega}} = -\frac{1 + \sqrt{6}z}{\sqrt{2} + \sqrt{3}z},$$

$$\frac{g_{N\phi}}{g_{N\omega}} = -\frac{\sqrt{6}z - 1}{\sqrt{2} + \sqrt{3}z}.$$



$$U_\Lambda(\rho_0) = -U_\Sigma(\rho_0) = -30 \text{ MeV}, U_\Xi(\rho_0) = -14 \text{ MeV}$$



Letter

Correlation of the hyperon potential stiffness with hyperon constituents in neutron stars and heavy-ion collisions

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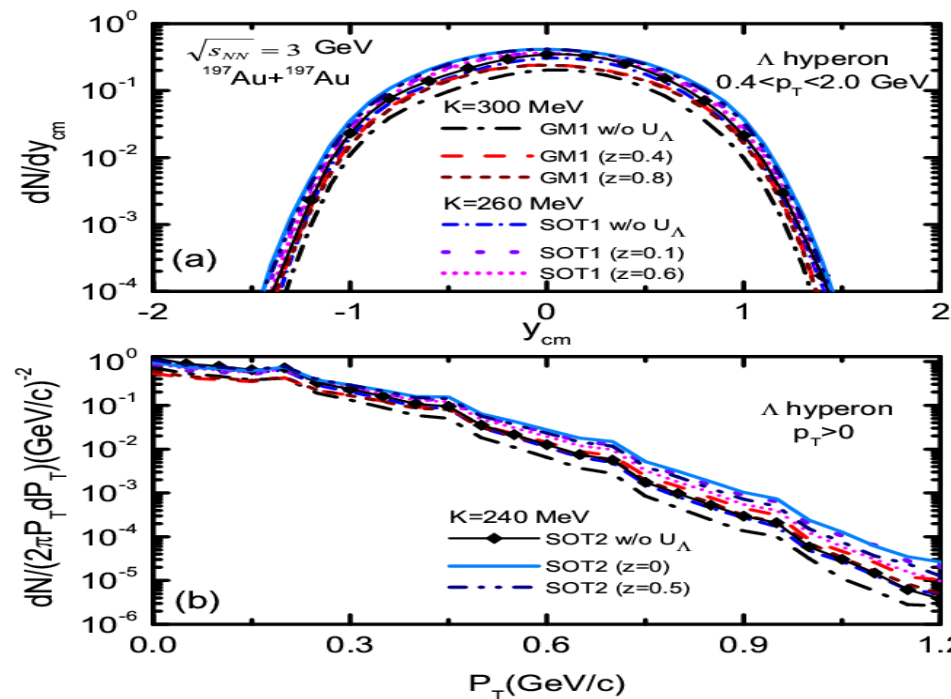
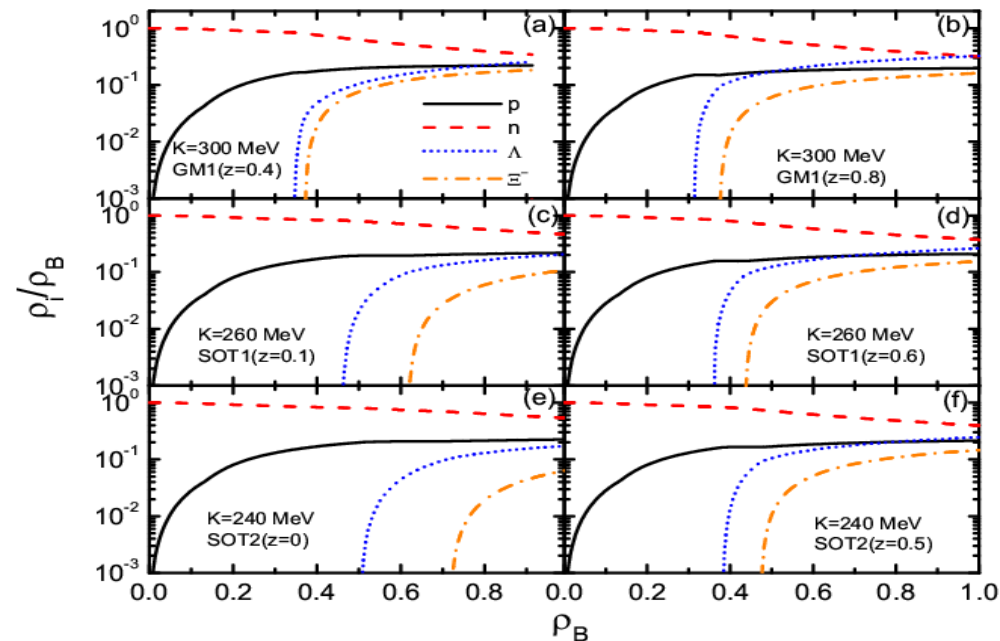
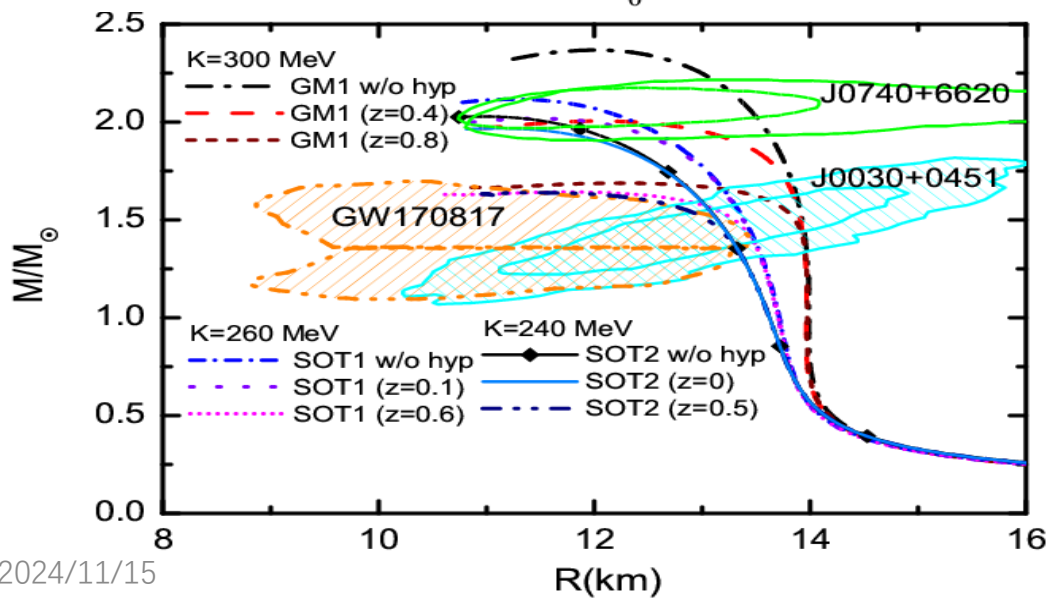
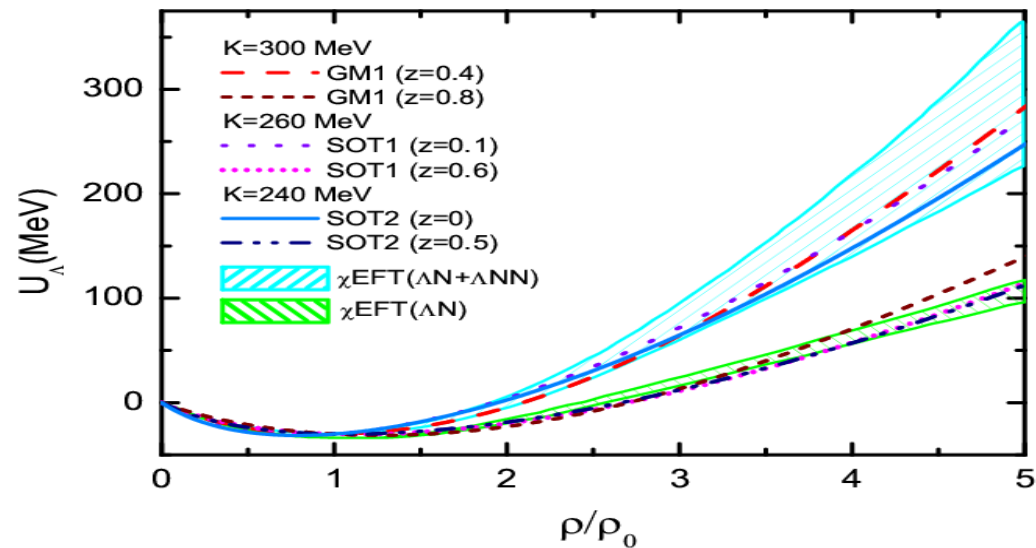
<sup>c</sup> School of Physics, Southeast University, Nanjing 211189, China



**LQMD.RMF**

# Correlation of the hyperon potential stiffness with hyperon constituents in neutron stars and heavy-ion collisions

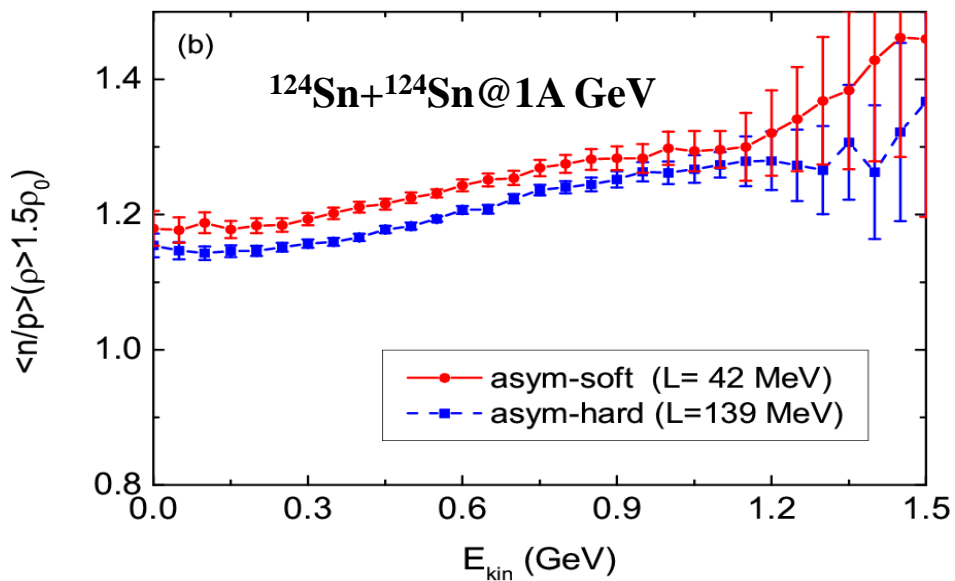
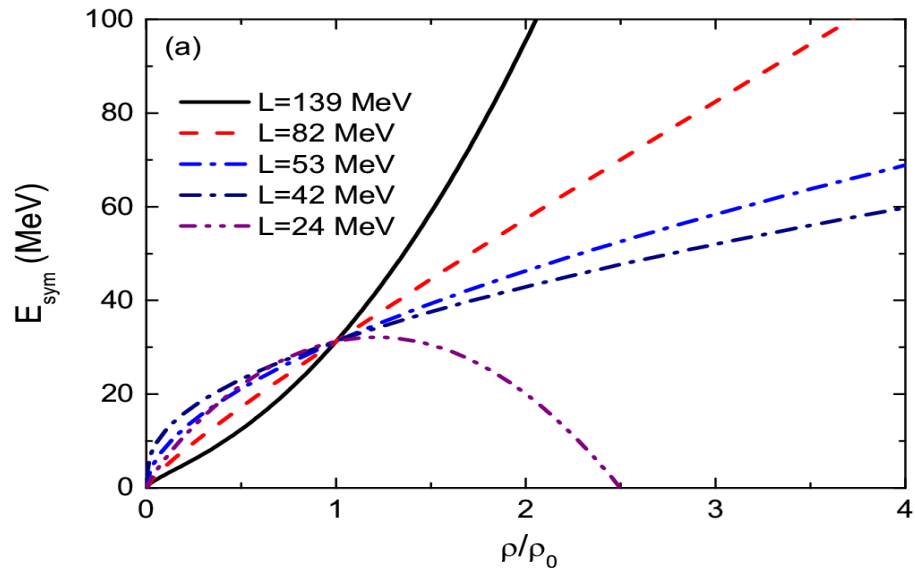
Si-Na Wei, ZQF, Wei-Zhou Jiang, PLB 853 (2024) 138658



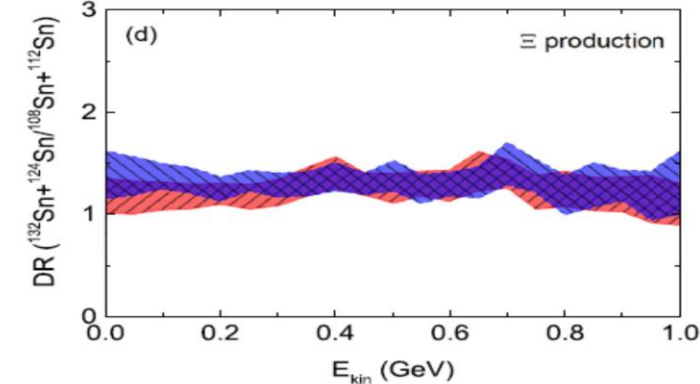
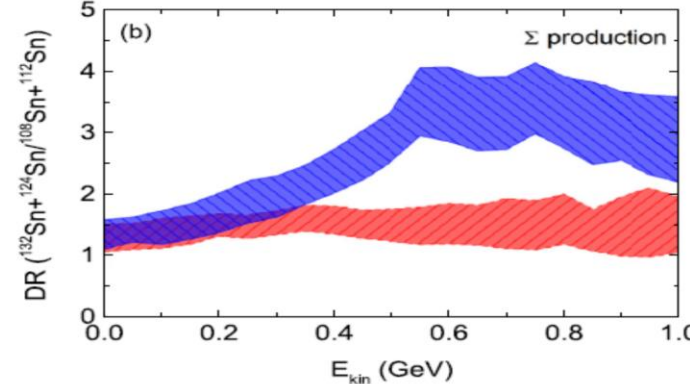
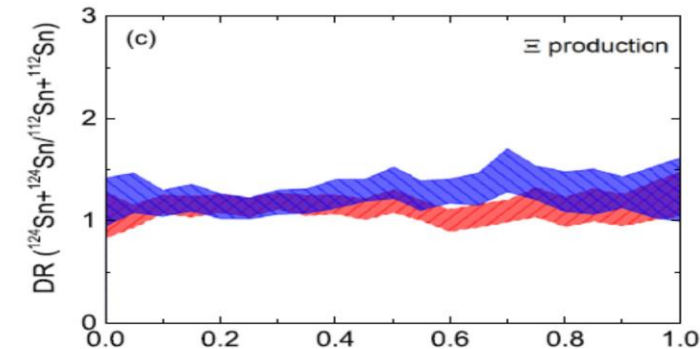
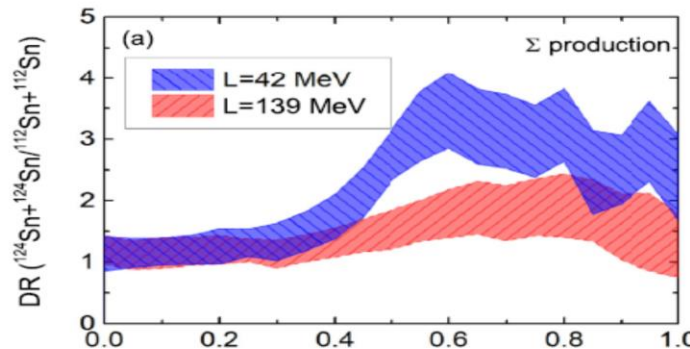
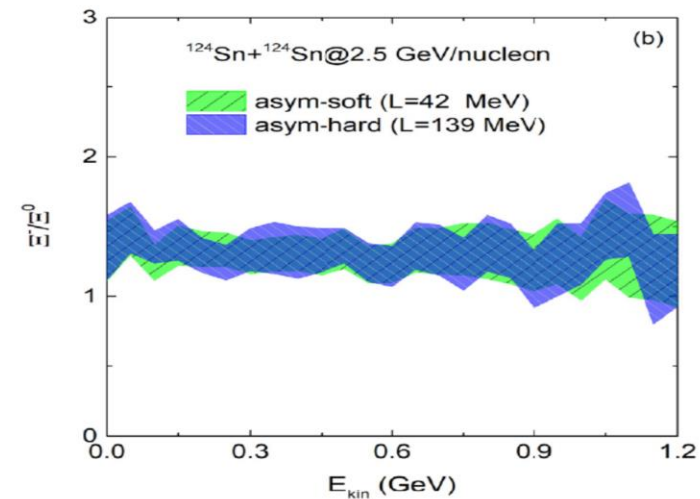
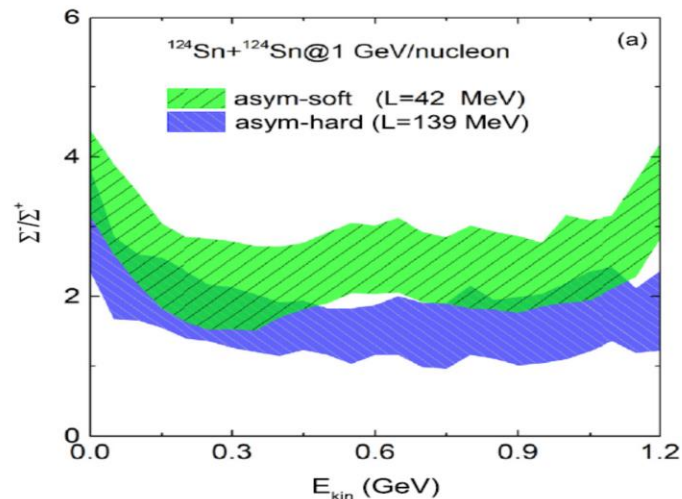
Probing the high-density symmetry energy from subthreshold hyperon production in heavy-ion collisions

Zhao-Qing Feng

School of Physics and Optoelectronics, South China University of Technology, Guangzhou 510640, China



# High-density symmetry energy from hyperon production in heavy-ion collisions, **Physics Letters B 846 (2023) 138180**





# IV. 超核产生动力学研究

## Kinetic approach for cluster production

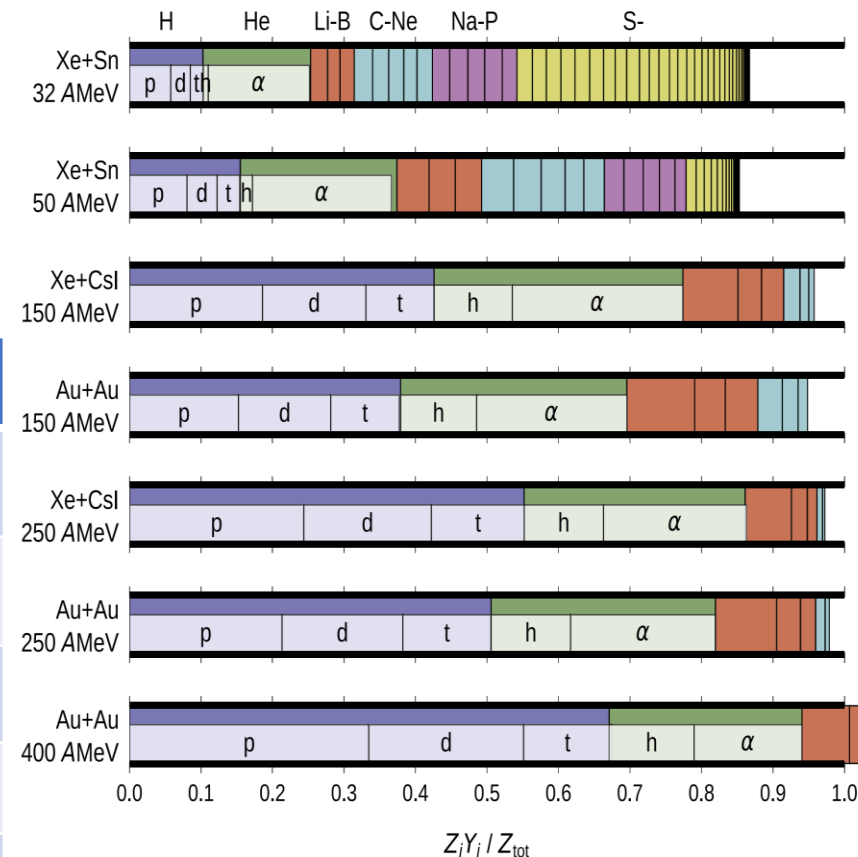
P. Danielewicz, G. F. Bertsch, Nuclear Physics A 533 (1991) 712-748

Akira Ono, Prog. Part. Nucl. Phys. 105, 139-179 (2019)

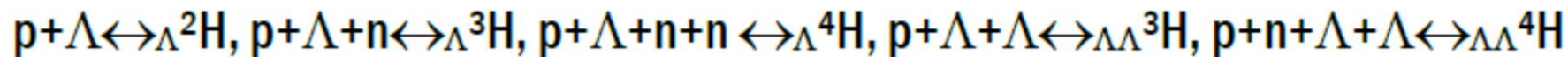
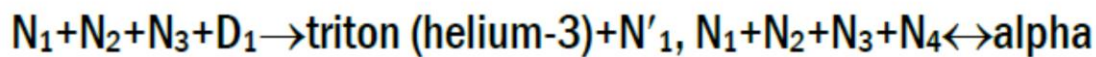
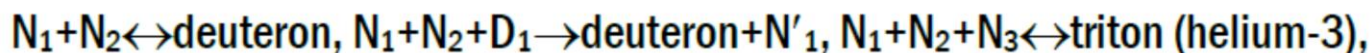
R. Wang, Y. G. Ma, L. W. Chen et al., Phys. Rev. C 108, L031601 (2023)

Hui-Gan Cheng, Zhao-Qing Feng, Phys. Rev. C 109, L021602 (2024)

Year	models	Author(s)	Cluster(s)	Energy	Treatment(s)
1991	pBUU	P. Danielewicz et al.	$d, t, h$	fermi /intermediate energies	kinetic, Mott cut
2013	AMD-cluster	A. Ono	$2N, 3N, \alpha$	fermi /intermediate energies	kinetic, fermionic mean field
2021	SMASH	J. Staudenmaier et al.	$d$	GeV and higher	kinetic
2022	PHQMD	G. Coci et al.	$d$	GeV and higher	kinetic
2023	IBUU	R. Wang et al.	$d, t, h, \alpha$	intermediate energies	kinetic, Mott cut
2023	LQMD	H. G. Cheng and Z. Q. Feng	$d, t, h, \alpha$	fermi /intermediate energies	Kinetic, binding energy, Pauli effects



**Clusters are produced by multinucleon or nucleon-cluster collisions**



...

2024/11/15

$$\frac{d\sigma}{d\Omega} = P(C_1 + C_2 \rightarrow C_3 + C_4) \times \frac{v_{\tilde{p}_{\text{rel}}}}{v} \frac{|\partial e(k)/\partial k|_{k=\tilde{p}_{\text{rel}}}}{|\partial H(p_f)/\partial p_f|_{p_f=p_{\text{rel}}}} \frac{p_{\text{rel}}^2}{\tilde{p}_{\text{rel}}^2} \left[ \frac{d\sigma_{\text{NN}}}{d\Omega} \right]_{\tilde{p}_{\text{rel}}}$$



# Kinetic approach for cluster production (LQMD.cluster)

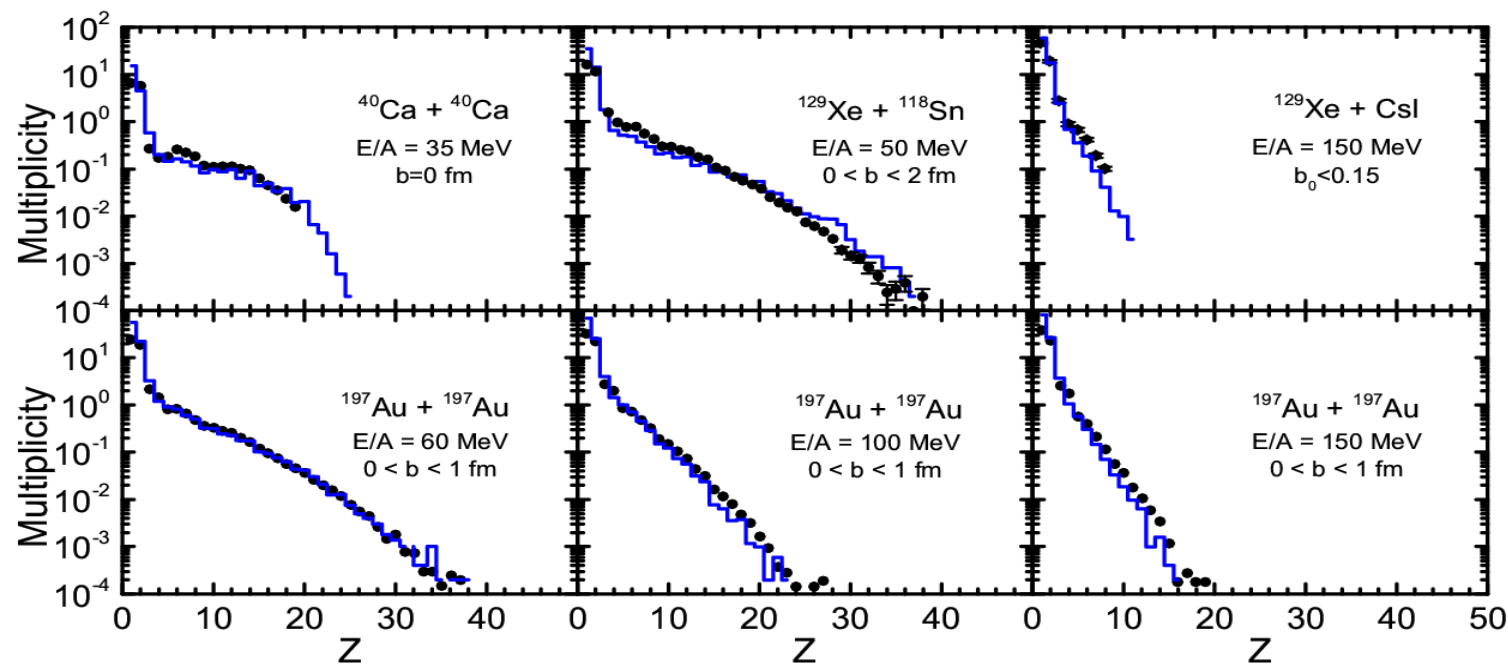
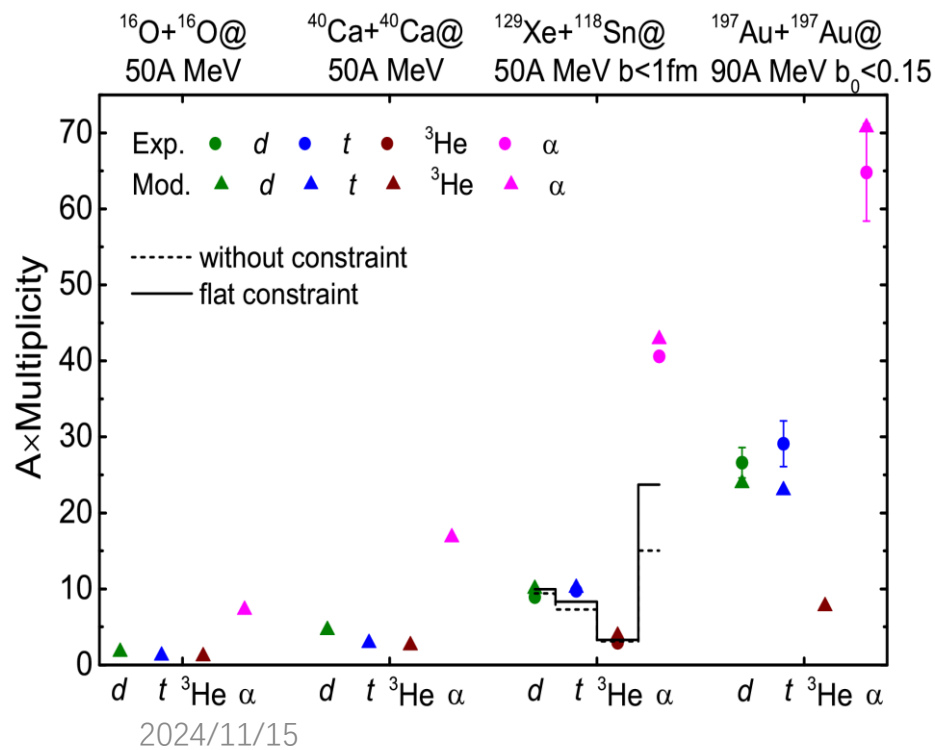
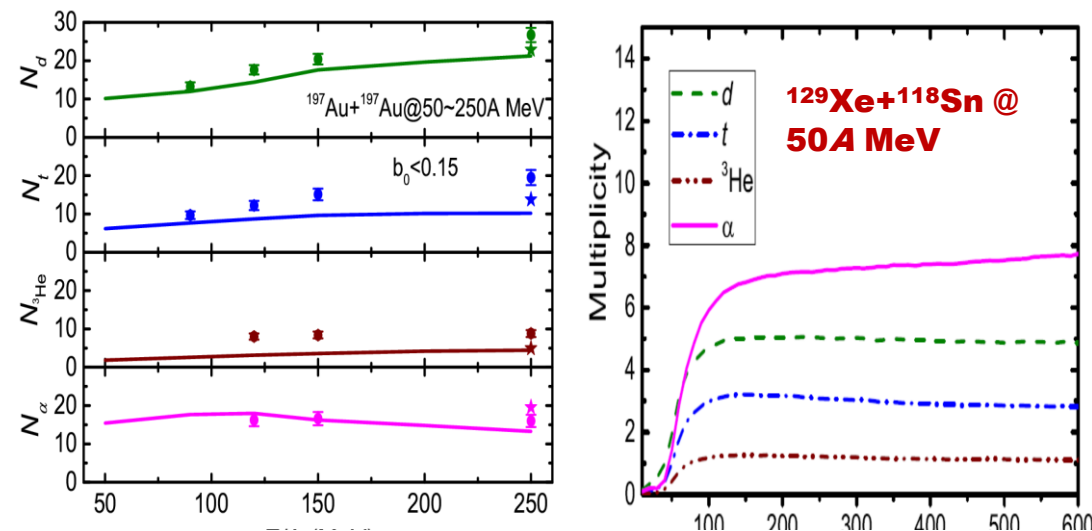
## Novel approach to light-cluster production in heavy-ion collisions

Hui-Gan Cheng and Zhao-Qing Feng\*

School of Physics and Optoelectronics, South China University of Technology, Guangzhou 510640, China

(Received 8 November 2023; accepted 25 January 2024; published 15 February 2024)

$$\begin{aligned}
 H = & \sum_i \frac{\mathbf{p}_i^2}{2m} + \frac{\alpha}{2} \sum_{\substack{i,j \\ j \neq i}} \frac{\rho_{ij}}{\rho_0} + \frac{\beta}{1+\gamma} \sum_i \left( \sum_{\substack{j,j \neq i}} \frac{\rho_{ij}}{\rho_0} \right)^\gamma \\
 & + \frac{C_{sym}}{2} \sum_{\substack{i,j \\ j \neq i}} t_{z_i} t_{z_j} \frac{\rho_{ij}}{\rho_0} + \frac{g_{sur}}{2} \sum_{\substack{i,j \\ j \neq i}} \left[ \frac{3}{2L} - \left( \frac{\mathbf{r}_i - \mathbf{r}_j}{2L} \right)^2 \right] \frac{\rho_{ij}}{\rho_0} \\
 & + \sum_i^{N_C} E_{z.p.}^i + \sum_i^{N_d} V_{corr} e^{-r_i^2/4L}
 \end{aligned}$$



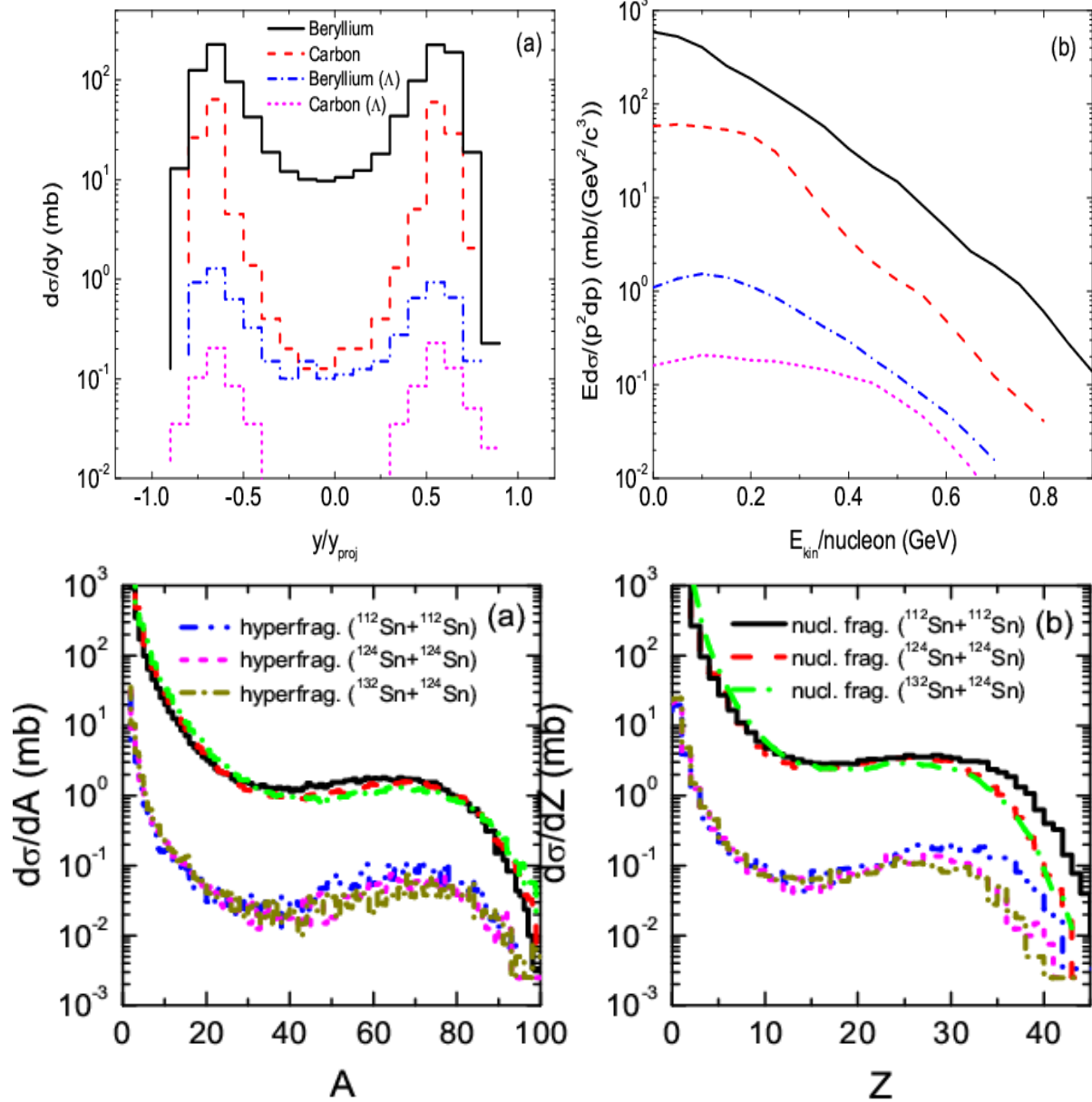
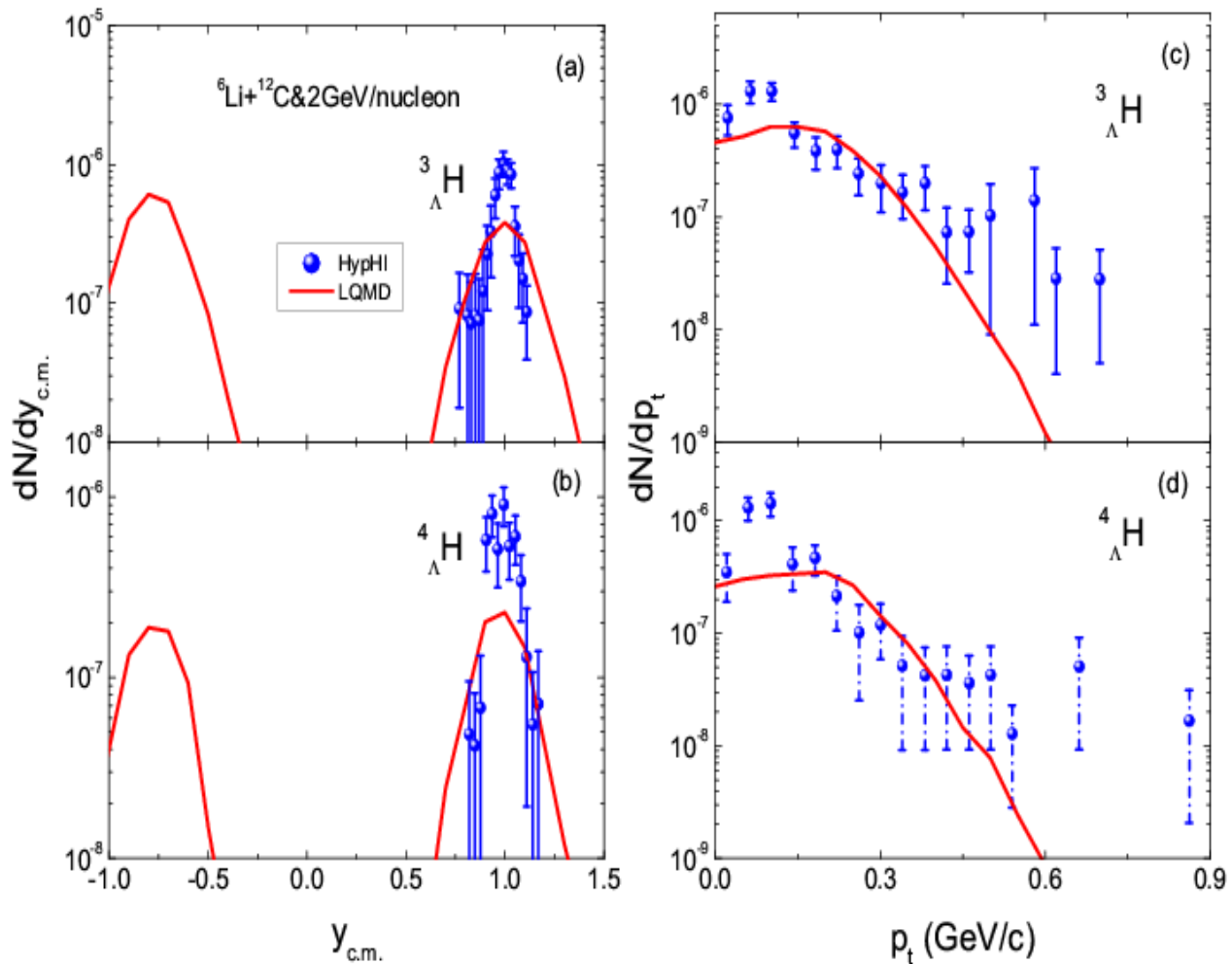
# Hypernuclide production via HICs (Wigner density approach)

Z. Q. Feng, Phys. Rev. C 102, 044604 (2020)

Data: C. Rappold et al., (HypHI collaboration)

Phys. Lett. B 747, 129 (2015)

$^{124}\text{Sn}+^{124}\text{Sn}@2A\text{ GeV}$



# Multi-strangeness hypernuclide production

H.G. Cheng, Z. Q. Feng, Phys. Lett. B 824 (2022) 136849

$^{197}\text{Au} + ^{197}\text{Au} @ 3A \text{ GeV}$

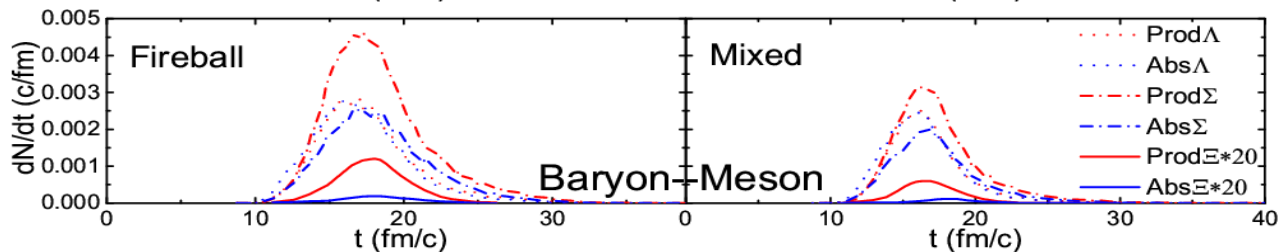
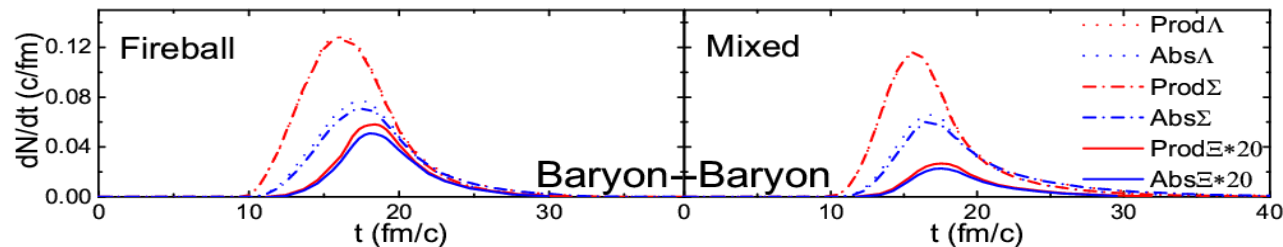
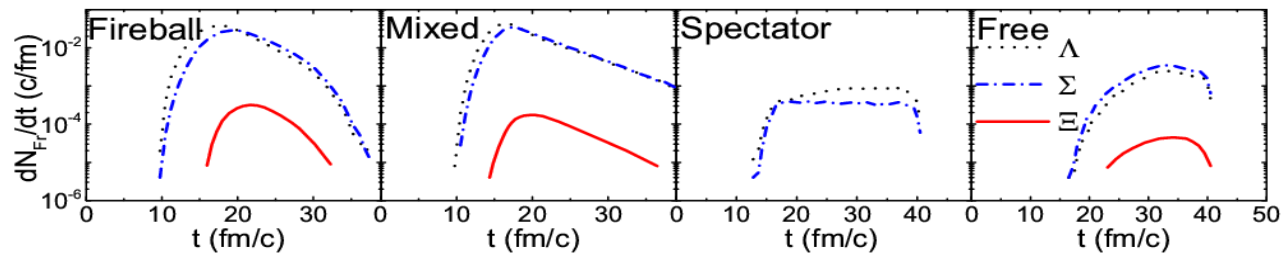
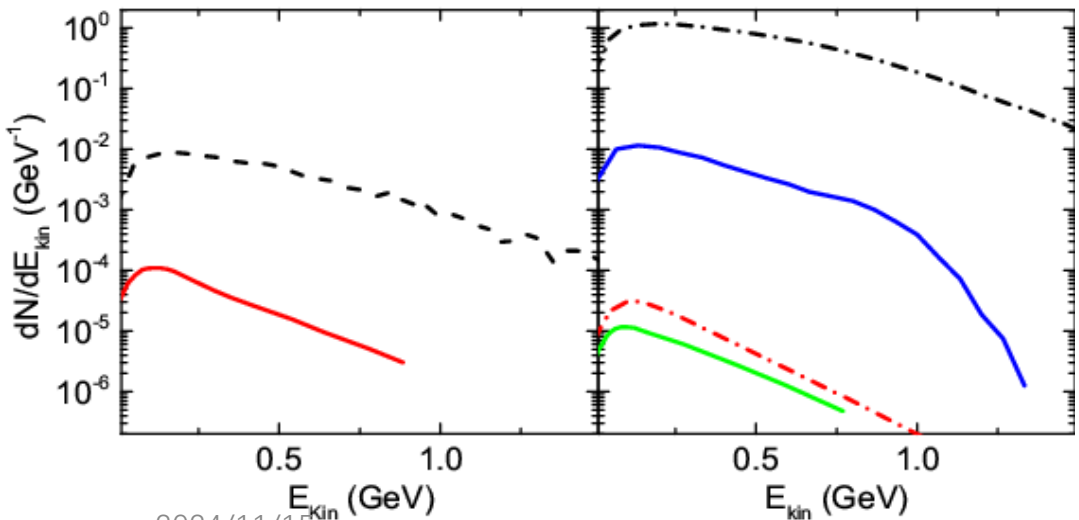
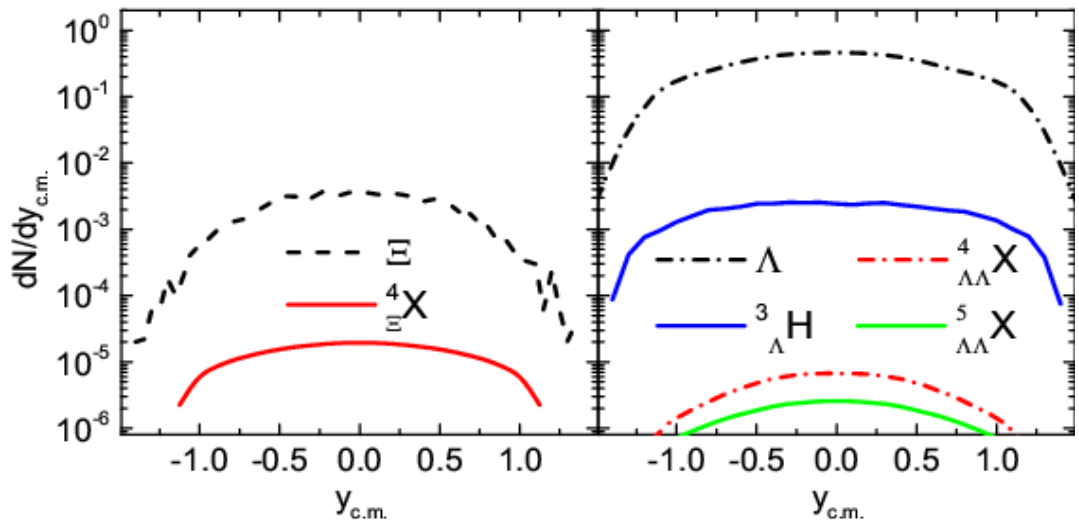


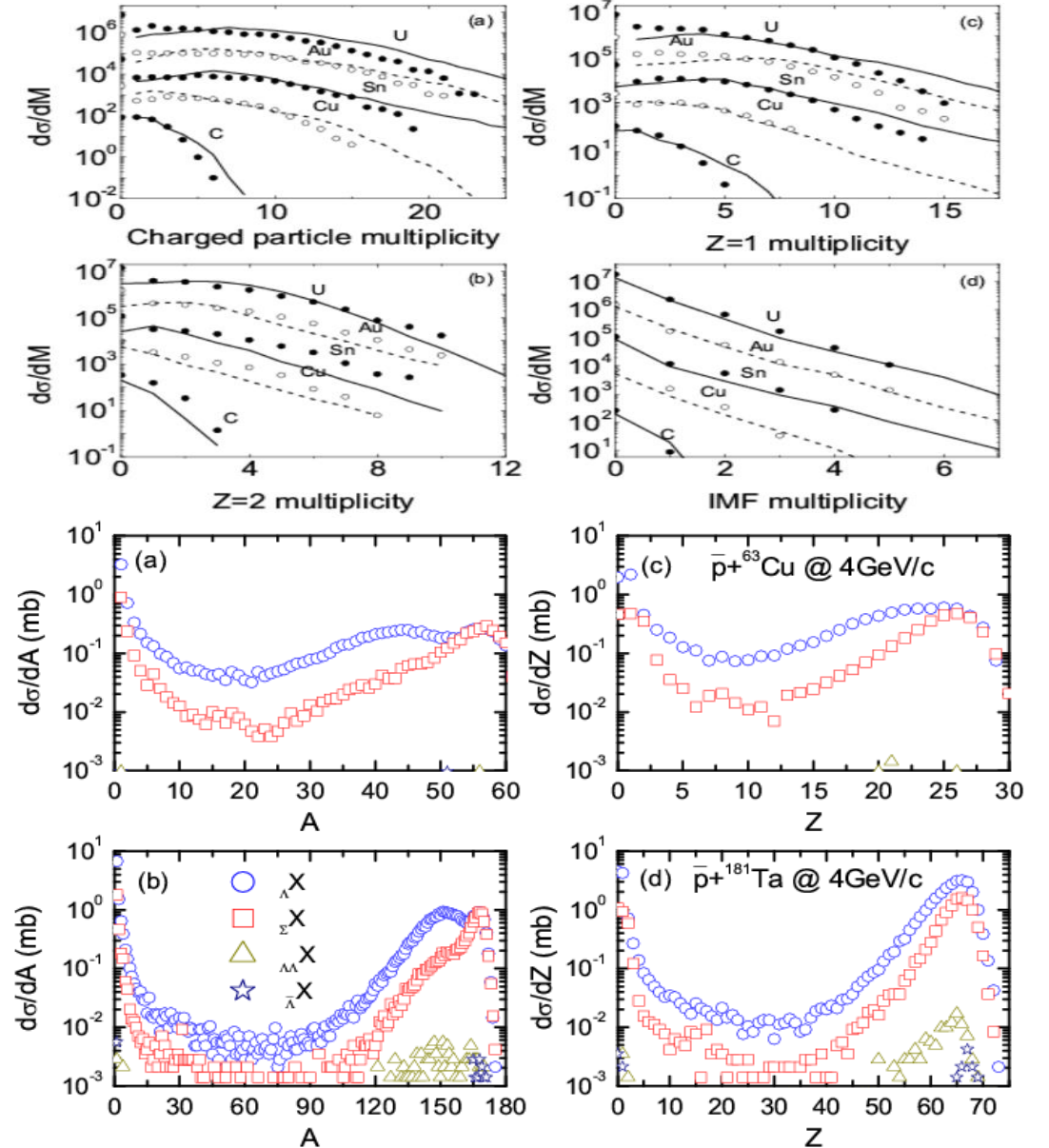
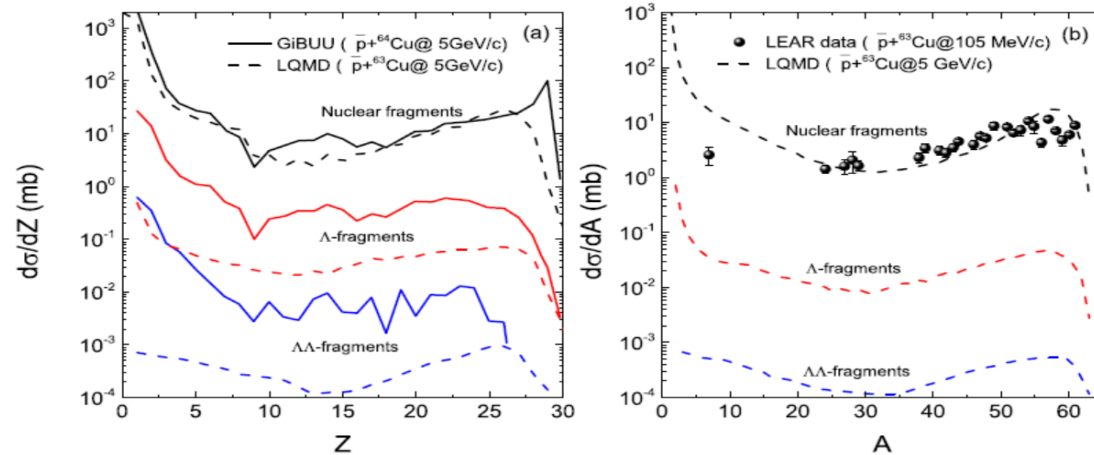
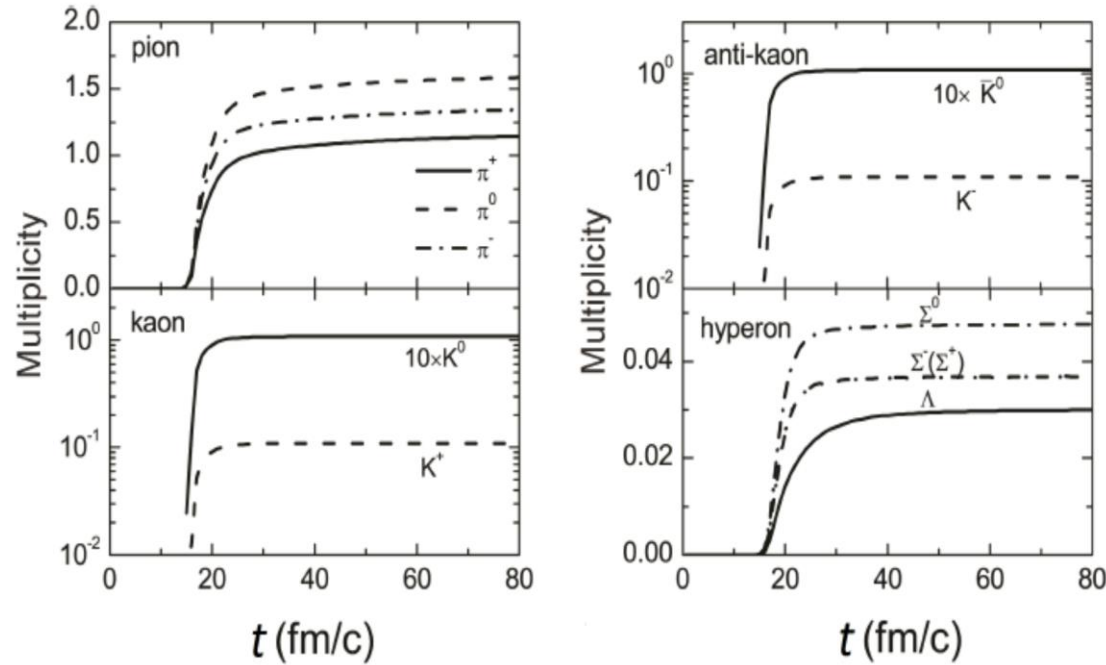
TABLE I. Comparison between cross sections of double lambda hypernuclei calculated with  $r_0 = 3.5 \text{ fm}$  for  $\Lambda$  in  $^{197}\text{Au} + ^{197}\text{Au}$  and  $^{40}\text{Ca} + ^{40}\text{Ca}$  collisions at  $3A \text{ GeV}$

Hypernuclei	Cross sections (mb)	
	$^{197}\text{Au} + ^{197}\text{Au}$	$^{40}\text{Ca} + ^{40}\text{Ca}$
${}^4_{\Lambda\Lambda}\text{H}$	$2.6 \times 10^{-2}$	$1.0 \times 10^{-4}$
${}^4_{\Lambda\Lambda}\text{He}$	$1.0 \times 10^{-2}$	$\sim 10^{-5}$
${}^5_{\Lambda\Lambda}\text{H}$	$5.9 \times 10^{-3}$	$\sim 10^{-5}$
${}^5_{\Lambda\Lambda}\text{He}$	$5.1 \times 10^{-3}$	$\sim 10^{-5}$
${}^5_{\Lambda\Lambda}\text{Li}$	$1.4 \times 10^{-3}$	$\sim 10^{-6}$
${}^6_{\Lambda\Lambda}\text{He}$	$2.2 \times 10^{-3}$	$\sim 10^{-6}$
${}^7_{\Lambda\Lambda}\text{He}$	$6.8 \times 10^{-4}$	$\sim 10^{-6}$

# IV. HIAF装置 $\pi$ 介子和反质子束流相关物理讨论

(Hyper) nuclear fragments with antiproton induced reactions

Zhao-Qing Feng, Physical Review C 101, 064601 (2020); 93, 041601(R) (2016)





Nuclear fragmentation and charge-exchange reactions induced by pions in the  $\Delta$ -resonance region

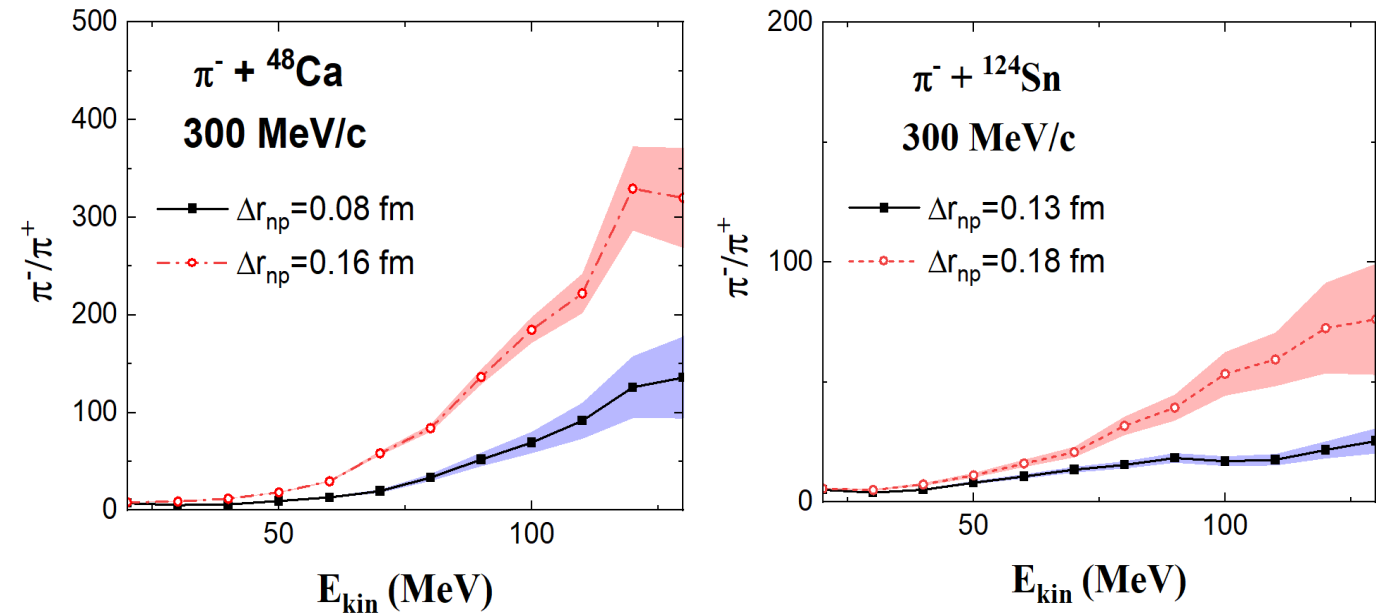
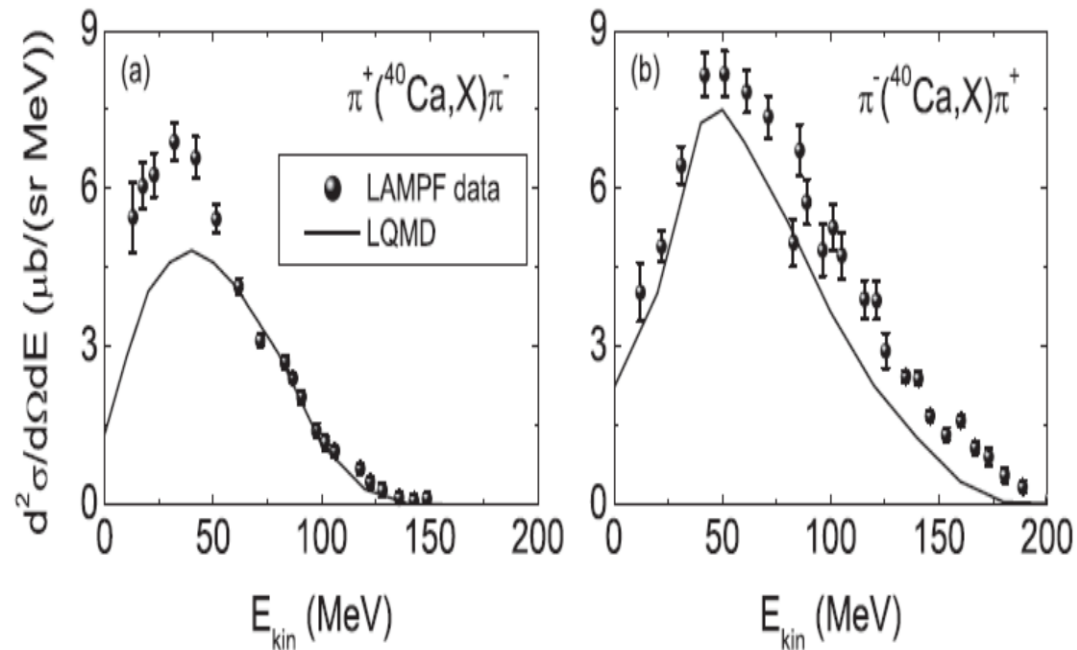
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(Received 5 September 2016; revised manuscript received 11 October 2016; published 18 November 2016)

The dynamics of the nuclear fragmentations and the charge exchange reactions in pion-nucleus collisions near the  $\Delta(1232)$  resonance energies has been investigated within the Lanzhou quantum molecular dynamics transport model. An isospin-, momentum-, and density-dependent pion-nucleon potential is implemented in the model, which influences the pion dynamics, in particular the kinetic energy spectra, but weakly impacts the fragmentation mechanism. The absorption process in pion-nucleon collisions to form the  $\Delta(1232)$  resonance dominates the heating mechanism of the target nucleus. The excitation energy transferred to the target nucleus increases with the pion kinetic energy and is similar for both  $\pi^-$ - and  $\pi^+$ -induced reactions. The magnitude of fragmentation of the target nucleus weakly depends on the pion energy. The isospin ratio in the pion double-charge exchange is influenced by the isospin ingredient of target nucleus.

DOI: 10.1103/PhysRevC.94.054617



## 基于HIAF集群的高强度缪子、反质子次级束产生及其物理研究展望

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5. 中山大学物理学院, 广州 510275;

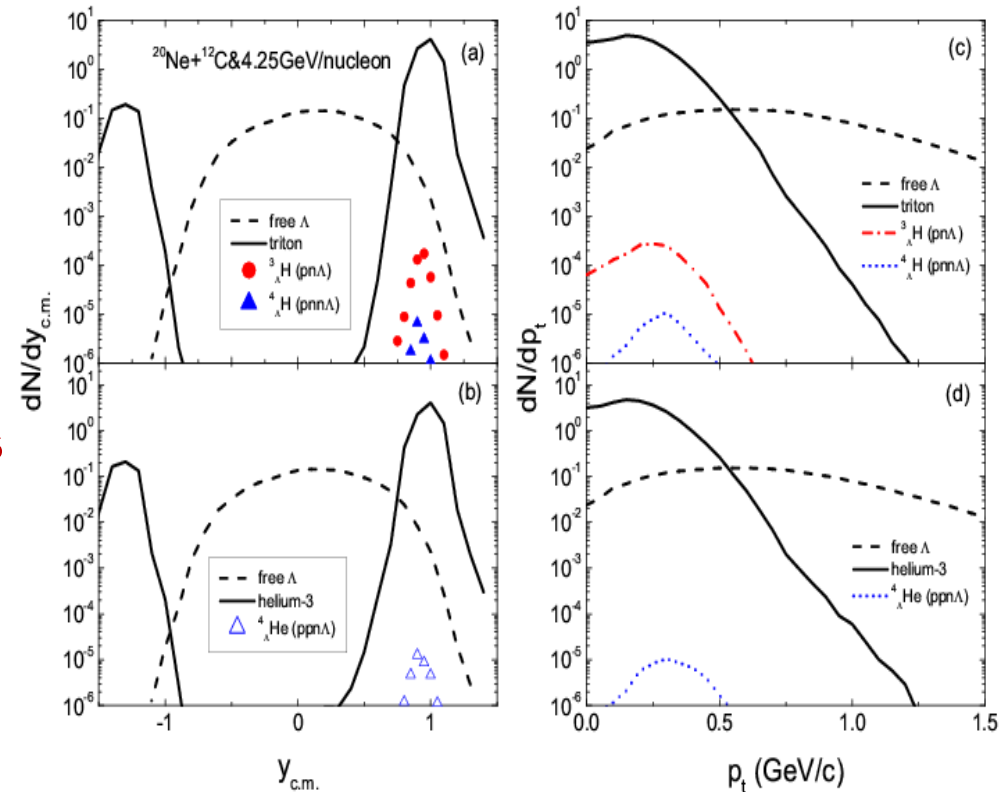
6. 中国科学院高能物理研究所, 北京 100049;

7. 华南理工大学物理与光电学院, 广州 510641

\*联系人, E-mail: sunzhy@impcas.ac.cn

# VI. 总结和展望

- The Extremely proton-rich/neutron-rich hypernucleides might be created via heavy-ion collisions at HIAF energies, e.g.,  ${}^3_{\Lambda}\text{H}$  and  ${}^4_{\Lambda}\text{H}$  production in the reaction of  ${}^{20}\text{Ne}+{}^{12}\text{C}$  at HIAF.
- The high-density symmetry probes single and double ratios of  $\Sigma^-/\Sigma^+$ (double ratio) via the isotopic reactions  ${}^{112}\text{Sn}+{}^{112}\text{Sn}$  and  ${}^{124}\text{Sn}+{}^{124}\text{Sn}$ , in particular above 0.4 GeV.
- The 3-body interaction potentials, e.g.,  $\Lambda\text{NN}, \Sigma\text{NN}, \Xi\text{NN}$  etc, might be constrained via heavy-ion collisions at HIAF.
- Antiproton and pion beams are being expected at the HIAF facility for hypernuclear physics, in-medium properties of hadrons, neutron-skin thickness, equation of state.



Thanks for your attention!