# 低能中微子核子散射

(Low-energy neutrino-nucleon scattering in ChPT)

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### Introduction

2 Neutral current elastic neutrino-nucleon scattering

**3** Weak single pion production off the nucleon

### Summary and Outlook

# I. Introduction

# **Neutrino physics**

### □ Report of the 2023 P5



Reveal the Secrets of the Higgs Boson

Pursue Quantum Imprints of New Phenomena

#### Understand What Drives Cosmic Evolution

### □ Elucidate the mysteries of neutrinos

- 🛯 Abroad: DUNE, IceCube-Gen2, NOνA, T2K, LEGEND , XLZD, nEXO, ...
- Domestic: JUNO, JUNO-TAO, PandaX-xT, CDEX-1T, CNUF ...

#### [https://www.usparticlephysics.org/2023-p5-report/]

## Neutrino interaction with matter

### $\hfill\square$ At the heart of many interesting and relevant physical phenomena

[Neutrinos in particle physics , astronomy and cosmology, Z-Z. Xing and S. Zhou, 2010]



### Neutrino-nucleon scattering:



 $\rightarrow$  a bridge connecting hadron physics and nuclear physics  $\rightarrow$  Important contribution to the inclusive

neutrino-nuclei ( $\nu A$ ) cross section

### Processes of neutrino-nucleon scattering

#### □ Two categories of processes:

Charged-Current (CC) & Neutral-Current (NC) induced.

### □ Different processes in different energy regions



Total cross section per nucleon (Prediction by NUANCE generator).

- Solution Charged current: **CCQE**  $\implies$  **IS** (RES,CC1 $\pi$ ,···)  $\implies$  **DIS**
- $\bowtie$  Neutral current : NCE  $\implies$  IS (RES,NC1 $\pi$ ,  $\cdots$ )  $\implies$  DIS

### Processes of neutrino-nucleon scattering

### □ CC processes:



CCQE

IE

DIS

### □ NC processes:



## II. Neutral current elastic $\nu N$ scattering

J. M. Chen, Z. R. Liang and DLY, Front. Phys. (Beijing) 19 (2024) 6, 64202

□ Low energies:

NCE: 
$$\nu + N \rightarrow \nu + N$$
, CCQE:  $\nu_{\ell} + N \rightarrow \ell + N$ 

NCE processes are sensitive both to isovector and isoscalar weak current!

 $\hfill\square$  Strangeness contribution to the nucleon spin  $\Delta s = G^s_A(Q^2=0)$ 

- $\blacksquare$  1980s, the E734 experiment at BNL:  $0.45 \leq Q^2 \leq 1.05~{\rm GeV}^2$  [Ahrens et al., PRD1985]
- Solution 2010 & 2015, the MiniBooNE experiment at FNAL:  $Q^2 \le 2 \text{ GeV}^2$ [Aguilar-Arevalo et al., PRD2010 & PRD2015)]
- The future MicroBooNE experiment in Argon:  $0.1 \le Q^2 \le 1 \text{ GeV}^2$  [Ren, JPS Conf. Proc. 37, 020309 (2022).]

□ Various parametrizations for form factors

- Dipole parametrization
- z expansion

rg ....

#### A model-independent and systematical study is needed!

### Kinematics & amplitude structure

 $\Box$  Kinematics:  $\nu(q_1) + N(p_1) \rightarrow \nu(q_2) + N(p_2)$ 



$$\mathcal{M} = -\frac{G_F}{\sqrt{2}} L_\mu H^\mu \; ,$$

Leptonic part:  $L_{\mu} = \bar{\nu}(q_2)\gamma_{\mu}(1-\gamma_5)\nu(q_1)$ , Hadronic part:  $H^{\mu} = \langle N(p_2)|\mathcal{J}_{NC}^{\mu}(0)|N(p_1)\rangle$ .

□ Hadronic amplitude  $\rightarrow$  6 form factors (FFs) Isospin structure: isovector (V) & isoscalar (S)

$$\begin{split} H^{\mu} &= \chi_{f}^{\dagger} \left[ \frac{\tau_{a}}{2} H_{V}^{\mu} + \frac{\tau_{0}}{2} H_{S}^{\mu} \right] \chi_{i} , \quad a = 3, \\ H_{V}^{\mu} &= (1 - 2\sin^{2}\theta_{W}) V_{V}^{\mu} - A_{V}^{\mu} , \quad H_{S}^{\mu} = -2\sin^{2}\theta_{W} V_{S}^{\mu} \end{split}$$

Lorentz decomposition:

$$\begin{split} V_{V,S}^{\mu} = & \bar{\mathbf{u}}(p_2) \left[ \gamma^{\mu} F_1^{V,S}(t) + \frac{i}{2m_N} \sigma^{\mu\nu} q_{\nu} F_2^{V,S}(t) \right] \mathbf{u}(p_1), \\ A_V^{\mu} = & \bar{\mathbf{u}}(p_2) \left[ \gamma^{\mu} \gamma_5 G_A(t) + \frac{q^{\mu}}{m} \gamma_5 G_P(t) \right] \mathbf{u}(p_1) \; . \end{split}$$

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## Form factors from BChPT

 $\Box$  Calculation up to  $\mathcal{O}(p^3)$ 



#### □ Form factors in a chiral series

$$\begin{split} F_1^V(t) =& 1 - 2d_6t + F_1^{V,\text{loops}} + F_1^{V,\text{wf}} ,\\ F_2^V(t) =& c_6 + 2d_6t + F_2^{V,\text{loops}} + F_2^{V,\text{wf}} ,\\ F_1^S(t) =& 1 - 4d_7t + F_1^{S,\text{loops}} + F_2^{S,\text{wf}} ,\\ F_2^S(t) =& (c_6 + 2c_7) + 4d_7t + F_2^{S,\text{loops}} + F_2^{S,\text{wf}} ,\\ G_A(t) =& g + (4d_{16}M^2 + d_{22}t) + G_A^{\text{loops}} + G_A^{\text{wf}} ,\\ G_P(t) =& \frac{2gm_N^2}{M^2 - t} + \frac{4m_N^2M^2(2d_{16} - d_{18})}{M^2 - t} + \frac{4gm_N^2M^2\ell_4}{F^2(M^2 - t)} - 2m_N^2d_{22} \\ &\quad - \frac{4gm_N^2M^2\Big[M^2\ell_3 + (M^2 - t)\ell_4\Big]}{F^2(M^2 - t)^2} + G_P^{\text{loops}} + G_P^{\text{wf}} , \end{split}$$

#### Remarks:

- Wave function renormalization
- ${\tt IS}$  UV divergences: dimensional regularization (DR) with  $\overline{\rm MS}\mbox{--}1~(\widetilde{\rm MS})$  subtraction
- PCB terms: EOMS scheme

## NCE scattering within EOMS scheme

**Essence:** two-step renormalization  $(\widetilde{MS}+finite)$ 

1. UV subtraction:  

$$m = m^{r}(\mu) + \beta_{m} \frac{R}{16\pi^{2}F^{2}} ,$$

$$g = g^{r}(\mu) + \beta_{g} \frac{R}{16\pi^{2}F^{2}} ,$$

$$c_{i} = c_{i}^{r}(\mu) + \beta_{c_{i}} \frac{R}{16\pi^{2}F^{2}} ,$$

$$d_{j} = d_{j}^{r}(\mu) + \beta_{d_{j}} \frac{R}{16\pi^{2}F^{2}} .$$

2. Finite subtraction:  $m^{r}(\mu) = \widetilde{m} + \frac{\widetilde{\beta}_{m}}{16\pi^{2}F^{2}} ,$   $g^{r}(\mu) = \widetilde{g} + \frac{\widetilde{\beta}_{g}}{16\pi^{2}F^{2}} ,$   $c_{i}^{r}(\mu) = \widetilde{c}_{i} + \frac{\widetilde{\beta}_{c_{i}}}{16\pi^{2}F^{2}} .$ 

### Advantages:

- ${\tt I}{\tt S}{\tt S}$  Power counting is restored  $\longrightarrow$  predictive power
- Respect original analytic properties → spectroscopy (poles and cuts), chiral extrapolation, finite volume corrections
- Fast convergency behaviour in many cases, w.r.t. IR, HB, etc

## **Observables for physical processes**

#### Differential cross sections

$$\frac{\mathrm{d}\sigma}{\mathrm{d}Q^2} = \frac{G_F^2 m_N^2}{8\pi E_\nu^2} \bigg[ A(Q^2) \pm \frac{(s-u)}{m_N^2} B(Q^2) + \frac{(s-u)^2}{m_N^4} C(Q^2) \bigg]$$

Convenient scalar functions A, B and  $C: (\eta = Q^2/4m_N^2 \& \text{No } G_P \text{ for NCE})$   $A(Q^2) \equiv 4\eta \Big[ \mathcal{G}_A^2(Q^2) (1+\eta) + 4\eta \mathcal{F}_1(Q^2) \mathcal{F}_2(Q^2) - \Big( \mathcal{F}_1^2(Q^2) - \eta \mathcal{F}_2^2(Q^2) \Big) (1-\eta) \Big]$  $B(Q^2) \equiv 4\eta \ \mathcal{G}_A(Q^2) \Big( \mathcal{F}_1(Q^2) + \mathcal{F}_2(Q^2) \Big)$ 

$$C(Q^2) \equiv \frac{1}{4} \left[ \mathcal{G}_A^2(Q^2) + \mathcal{F}_1^2(Q^2) + \eta \mathcal{F}_2^2(Q^2) \right]$$

Relationship between isospin and physical bases

$$\begin{split} \mathcal{F}_{i}(t) &= \cos 2\theta_{W}F_{i}^{V}(t)\frac{\mathcal{C}_{3}}{2} - 2\sin^{2}\theta_{W}F_{i}^{S}(t)\frac{\mathcal{C}_{0}}{2} , \quad i = 1, 2, \\ \mathcal{G}_{j}(t) &= G_{j}(t)\frac{\mathcal{C}_{3}}{2} , \quad j = A, P, \end{split}$$

physical process	$\mathcal{C}_3$	$\mathcal{C}_0$	physical process	$\mathcal{C}_3$	$\mathcal{C}_0$
$\nu + p \rightarrow \nu + p$	1	1	$\nu+n \rightarrow \nu+n$	-1	1
$\bar{\nu} + p \rightarrow \bar{\nu} + p$	1	1	$\bar{\nu} + n \rightarrow \bar{\nu} + n$	$^{-1}$	1
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## **Differential cross section**

### Proton channels



- Sizeable Pauli blocking effects
- Contribution of strangeness axial form factor?

#### Neutron channels



- No experimental data
- Large deviation from the NuWro results

## **Total cross section**

### Order by order



Our ChPT results deviate from the NuWro ones for neutron channels
 Large difference between NuWro and GENIE due to nuclear effects

## III. Weak single pion production

[DLY, L. Alvarez-Ruso, A. N. Hiller Blin and M. J. Vicente Vacas, PRD2018] [DLY, L. Alvarez-Ruso and M. J. Vicente Vacas, PLB2019]

# Weak single pion production

□ Oscillation experiments (e.g. T2K)

► survival probability of  $\nu_{\mu}$ :  $P(\nu_{\mu}) = 1 - \sin^2 2\theta_{\mu\tau} \cdot \sin^2 \frac{\Delta m_{23}L}{E_{\nu}}$ 



#### □ Source of experimental uncertainties

#### **CC** 1*π*:

Solution  $\mathbb{C}$  CCQE-like events: misiden. of pion solution to be subtracted for a good  $E_{\nu}$ 



#### **NC** 1*π*:

series e-like background to  $\nu_{\mu} \rightarrow \nu_{e}$  searches improved at T2K with a  $\pi^{0}$  rejection cut



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### Isobar Models

 ${\tt ISS}~\Delta$  and heavier resonances  $\rightarrow$  nucleon-to-resonance form factors:

[e.g., Llewellyn Smith, Phys. Rep. 3 (1972)] [Fogli and Nardulli, Nucl. Phys. B160 (1979)] [Rein and Sehgal, Ann. Phys. (1981)]

- Real form factor from quark models
- $\bullet\,$  Conserved vector current  $\to\,$  related to electromagnetic ones extracted from electron scattering data
- PCAC  $\rightarrow$  off-diagonal Goldberger-Treiman (GT) relation for the axial couplings

#### Nonresonant mechanisms

[Fogli and Nardulli, Nucl. Phys. B160 (1979)] [Bijtebier, Nucl. Phys. B21 (1970)] [Alevizos et al., J. Phys. G 3(1977)]

### □ Hernandez-Nieves-Valverde (HNV) Model

- Final state interaction: imposing Watson's theorem [Alvarez-Ruso et al., Phys. Rev. D 93 (2016)]
- Unphysicsal spin-1/2 components: adding new contact terms

[Hernandez and Nieves, Phys. Rev. D (2017)]

### Other Models:

Dynamical model: coupled-channel Lippmann Schwinger equation

- Fulfilling Watson's theorem
- PCAC  $\rightarrow$  partially constrain the axial current in terms of  $\pi N$  scattering amplitude fitted to data [Nakamura, Kamano and Sato, Phys. Rev. D (2015)]
- ${\it I}{\it S}{\it S}$  Chiral effective model with  $\pi,$  N,  $\Delta$  together with  $\sigma,$   $\rho,$   $\omega$ 
  - Power counting only for tree diagrams

[Serot and Zhang, Phys. Rev. C (2012)]

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🕸 etc.
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#### Low energy regime:

Chiral symmetry + Power counting + Perturbative Unitarity

### □ Baryon Chiral Perturbation Theory (BChPT)

Low-Energy theorems (axial only) at threshold using heavy baryon formalism

[Bernard, Kaiser and Meißner, Phys. Lett. B (1994)]

 ${\it \blacksquare}$  Our work: One-loop analyses in relativistic BChPT with explicit  $\Delta {\sf s}$ 

[DLY, Alvarez-Ruso, Hiller-Blin and Vicent-Vacas, Phys. Rev. D (2018)]

[DLY, Alvarez-Ruso and Vicent-Vacas, Phys. Lett. B (2019)]

## Leptonic and Hadronic parts

### Physical channels (3 for CC & 4 for NC)



#### □ Amplitude structure:

- ${}^{\scriptstyle \rm I\!S\!S}$  One-boson approximation and  $k^2 \ll M_B^2$
- Solution  $L_{\nu}$  is well-known; Hadronic part  $H_{\mu}$  needs to be investigated.



### **Convenient isospin decomposition**

□ Isospin even (+), isospin odd (-), isoscalar (0)

$$\langle \pi^b N' | J^a_\mu(0) | N \rangle = \chi^\dagger_f \left[ \delta^{ba} H^+_\mu + i \epsilon^{bac} \tau^c H^- + \tau^b H^0_\mu \right] \chi_i$$

□ The physical amplitudes constructed from the isospin amplitudes

$$H_{\mu}$$
(physical process) =  $a_{+}H_{\mu}^{+} + a_{-}H_{\mu}^{-} + a_{0}H_{\mu}^{0}$ 

	Physical Process	$a_+$	$a_{-}$	$a_0$
	$Z^0 p  o p \pi^0$	1	0	1
NC	$Z^0 n \rightarrow n \pi^0$	1	0	$^{-1}$
NC	$Z^0 n \rightarrow p \pi^-$	0	$-\sqrt{2}$	$\sqrt{2}$
	$Z^0 p \rightarrow n \pi^+$	0	$\sqrt{2}$	$\sqrt{2}$
	$W^+p \rightarrow p\pi^+ / W^-n \rightarrow n\pi^-$	1	$^{-1}$	0
CC	$W^+n \rightarrow n\pi^+ / W^-p \rightarrow p\pi^-$	1	1	0
	$W^+n \rightarrow p\pi^0 / W^-p \rightarrow n\pi^0$	0	$\sqrt{2}$	0

□ The CC and NC amplitudes are related to each other For CC,  $H^{\pm}_{\mu} = \sqrt{2} \cos \theta_C (V^{\pm}_{\mu} - A^{\pm}_{\mu})$ ,  $H^0_{\mu} = 0$ . For NC,  $H^{\pm}_{\mu} = (1 - 2\sin^2 \theta_W) V^{\pm}_{\mu} - A^{\pm}_{\mu}$ ,  $H^0_{\mu} = (-2\sin^2 \theta_W) V^0_{\mu}$ 

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## The hadronic amplitude

**Tree diagrams up through**  $O(p^3)$ :



 $\Box$  All possible loop diagrams at  $O(p^3)$ :



89 diagrams & wave function renormalization & EOMS

## Necessity of the $\Delta$ resonance

#### $\square$ $\Delta$ is strongly coupled to the final $\pi N$ system

- $\blacksquare$  BR $(\Delta \to \pi N) \simeq 99.4\%$
- Solutions to  $\pi N$  threshold:  $\Delta = m_\Delta m_N \sim 300 \text{ MeV}$
- Strategy: the δ-counting

[Pascalutsa and Phillips, Phys. Rev. C67 (2012)]

- is hierachy of scales:  $M_{\pi} \sim p \ll \Delta \ll \Lambda \sim 4\pi F_{\pi}$
- server expanding parameter:  $\delta = \frac{\Delta}{\Lambda} \sim \frac{M_{\pi}}{\Delta} \sim \frac{p}{\Delta} \longrightarrow \frac{1}{p m_{\Delta}} = \frac{1}{p m_N \Delta} \sim p^{-\frac{1}{2}}$

Counting rule:

chiral order 
$$D = 4L + \sum_k kV^{(k)} - 2I_\pi - I_N - \frac{1}{2}I_\Delta$$

 ${f ar s}$  only trees of  $O(p^{3/2})$  and  $O(p^{5/2})$ 

in No loop diagrams with explicit  $\Delta$  up through  $O(p^3)$ 

The width effect

$$\frac{1}{m_{\Delta}^2 - s_{\Delta}} \to \frac{1}{m_{\Delta}^2 - im_{\Delta}\Gamma_{\Delta}(s_{\Delta}) - s_{\Delta}}$$

Energy dependent width  $\Gamma_{\Delta}(s_{\Delta})$  calculated in the same scheme

[Gegelia et al, Phys. Lett. B(2016)]

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## Cross sections for ${\bf CC}1\pi$

□ Fairly good agreement with the ANL data for most of the channels except for  $\nu_{\mu}n \rightarrow \mu^{-}n\pi^{+}$ 



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## Cross sections for $\mathbf{CC}1\pi$

### Order by order

- **Quite significant contribution when stepping from**  $O(p^2)$  and  $O(p^3)$
- Next-order effects could still be relevant (especially loops that  $\pi N$  can be put on-shell)



## Cross sections for $NC1\pi$

- The O(p<sup>3</sup>) ChPT calculation produces considerably larger cross sections with respect to the HNV model in all reaction channels.
- Nuwro and GIENE results agree with the ChPT ones with Δ contribution.
- Non-resonant contribution is sizeable, not accounted by Nuwro and GIENE.



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# IV. Summary and outlook

- □ Systematically study the NCE scattering and weak single pion production off the nucleon for the first time within covariant BChPT up to  $O(p^3)$ .
  - NCE: The X sections are useful for a precise determination of the strangeness axial vector form factor in future
  - Solution channels  $\mathbb{CC}_{1\pi}$  &  $\mathbb{NC}_{1\pi}$ : The  $\Delta$  contributes significantly to all production channels
  - NC1π: Non-resonant contribution is sizeable which is not implemented in events generators like NuWro and GIENE

Provide a well-founded low energy benchmark for phenomenological models aimed at the description of weak pion production in the broad kinematic range of interest for current and future neutrino-oscillation experiments.

#### Future application and perspective

- Applied to study various low-energy theorems
- Neutrino-nucleus scattering
- Implement ChPT results in events generator?

#### Thank you very much for your attention!

# Backup

## Valid energy region of BChPT

□ Valid energy region of BChPT



 ${\it I}$  Square of mom. transfer  $Q^2 \leq 0.2~{\rm GeV}^2 \longrightarrow$  neutrino energy  $E_{\nu} \leq 0.28~{\rm GeV}$ 

$$\sigma = \int_{-1}^{+1} \frac{\mathrm{d}\sigma}{\mathrm{d}Q^2} \frac{\mathrm{d}Q^2}{\mathrm{d}x} \mathrm{d}x}, \quad Q^2 = \frac{2m_N E_\nu^2}{2E_\nu + m_N} (1-x), \quad x = \cos\theta \ , \quad \theta \in [0,\pi]$$

## **Flux X-section**



### **Experimental data**

### **CC**1*π*







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### **Experimental data**



### Electroweak interaction in BChPT

### □ Covariant BChPT in SU(2) case.

🖙 Nucleonic Lagrangian

[Fettes et al Ann. Phys. (2000)]

Purely mesonic Lagrangian [Gasser and Leutwyler, Ann. Phys. (1984)] [Gasser et al., Nucl. Phys. B307 (1988)]

$$\mathcal{L}_{\pi} = \frac{F^2}{4} \operatorname{Tr}[\Delta_{\mu} U (\Delta^{\mu} U)^{\dagger} + \chi U^{\dagger} + U \chi^{\dagger}] + \sum_{j=3,4,6} \ell_j \mathcal{O}_j^{(4)}$$

#### Electro-weak interactions enter through external fields

[c.f. Scherer and Schindler, 2011, Springer]

 $\bowtie$  Charged weak bosons  $W^{\pm}$ :

$$r_{\mu} = 0, \quad l_{\mu} = -\frac{g}{\sqrt{2}} (V_{ud} W^{+}_{\mu} \tau_{+} + h.c.)$$

 $\bowtie$  Neural weak boson  $Z^0$ :

$$\begin{split} r_{\mu} &= e \tan(\theta_W) Z_{\mu}^0 \frac{\tau_3}{2}, \quad l_{\mu} = -\frac{g}{\cos(\theta_W)} Z_{\mu}^0 \frac{\tau^3}{2} + e \tan(\theta_W) Z_{\mu} \frac{\tau_3}{2}, \\ v_{\mu}^{(s)} &= \frac{e \tan(\theta_W)}{2} Z_{\mu}^0 \end{split}$$

## **Numerical settings**

 $\Box$  Energies considered for  $E_{\nu} \in [E_{\nu,th}, E_{\nu,\max} \equiv E_{\nu,th} + M_{\pi}]$ 

- Solution E.g.,  $E_{\nu,\max} = 415$  MeV for CC;  $E_{\nu,\max} = 289$  MeV for NC
- $\blacksquare$  Well below the  $\Delta$  peak  $\rightarrow \delta$ -counting is valid





Data for neutrino-induced single pion production off nucleons are very rare
 Values of the leading order constants

$F_{\pi}$	$M_{\pi}$	$m_N$	$m_{\Delta}$	$g_A$	$h_A$
92.21	138.04	938.9	1232  MeV	1.27	$1.43 \pm 0.02$

### Low energy constants beyond LO

Most of the LECs (16 out of 23) are previously determined from other processes or observables

	LEC	Value	Source	
$\mathcal{L}_{\pi\pi}^{(4)}$	$\bar{\ell}_6$	$16.5 \pm 1.1$	$\langle r^2  angle_\pi$ [Gasser, Leutwyler 1984]	
	$\tilde{c}_1$	$-1.00 \pm 0.04$		
	$\tilde{c}_2$	$1.01 \pm 0.04$	$\pi N$ contains (4) and (5) and (5)	
$\mathcal{L}_{-N}^{(2)}$	$\tilde{c}_3$	$-3.04 \pm 0.02$	$\pi IV$ SCattering [Alarcon et al. 2013 & Chen et al. 2013]	
$\pi I \mathbf{v}$	$\tilde{c}_4$	$2.02\pm0.01$		
	$\tilde{c}_6$	$1.35\pm0.04$	u and u to the second pocesses	
	$ ilde{c}_7$	$-2.68\pm0.08$	$\mu_p$ and $\mu_n$ [Bauer et al. 2012 & PDG2016]	
	$d_{1+2}^{r}$	$0.15 \pm 0.20$		
	$d_3^r$	$-0.23\pm0.27$		
$c^{(3)}$	$d_5^r$	$0.47\pm0.07$	$\pi N$ scattering [Alarcon et al. 2013 & Chen et al. 2013]	
$\mathcal{L}_{\pi N}$	$d_{14-15}^r$	$-0.50\pm0.50$		
	$d_{18}^{r}$	$-0.20\pm0.80$		
	$\tilde{d}_6^r$	-0.70	/m <sup>2</sup> \ IT     2014]	
	$d_7^r$	-0.47	VE/N [Fuchs et al. 2014]	
	$d_{22}^{r}$	$0.96 \pm 0.03$	$\langle r_A^2  angle_N$ [Yao et al. 2017]	
$\mathcal{L}^{(2)}_{\pi N\Delta}$	$b_1$	$(4.98 \pm 0.27)/m_N$	$\Gamma^{ m em}_{\Delta}$ [Bernard et al 2012]	
<b>T</b> I			and a state of the state	

lacksquare The remaining unknown LECs ightarrow set to natural size

 $d_j^r = 0.0 \pm 1.0 \text{ GeV}^{-2}$ ,  $j \in \{1, 8, 9, 14, 20, 21, 23\}$ 

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## **BChPT & PCB issue**



**Covariant ChPT including matter fields** (Baryons, D/B mesons,  $\Xi_{cc}$ )

 $\blacksquare$  Dimensional Regularization (DR) with standard  $\overline{\mathrm{MS}}$ -1 subtraction

A systematic power counting rule is lost due to the non-zero mass of matter fields in the chiral limit



# Solution I: HB

#### Essence: The full integral can be separated into Infared Singular and Regular parts.



#### □ Heavy baryon formalism (HB)

[Jenkins and Manohar, PLB255' 91]

#### A simultaneous expansion in external momenta and $1/m_B$

Non-covariant and slowly convergent in the threshold region. [N.Fettes,Ulf-G.Meissner and S.Steininger, NPA' 98, M.Mojzis, Eur.Phys.J.C2' 98]

Even divergent in the sub-threshold region (e.g. scalar form factor).

[V.Bernard,N.Kaiser and Ulf-G.Meissner,Int.J.Mod.Phys.E4' 95, T.Becher and H.Leutwyler,Eur.Phys.J.C9' 99]

Infrared Regularization (IR)
 Extended-on-mass-shell scheme (EOMS)

# Solution II: IR

#### Essence: The full integral can be separated into Infared Singular and Regular parts.



Heavy baryon formalism (HB)
 Infrared Regularization (IR)

[Jenkins and Manohar, PLB255' 91]

[T.Becher and H.Leutwyler, Eur. Phys. J.C9' 99]

#### The whole series of the regular part in the full integral are dropped.

- Scale-dependence: amplitude and observables. [T.Becher and H.Leutwyler, JHEP0106' 01]
- Unphysical cuts(u=0). [J.M.Alarcon, J.Martin Camalich, J.A.Oller and L.Alvarez-Ruso, PRC83' 11]

 ${\tt I}$  Bad predictions: e.g., huge Goldberger-Treiman relation violation (20-30%).

[J.M.Alarcon, J.Martin Camalich, J.A.Oller and L.Alvarez-Ruso, PRC83' 11]

#### Extended-on-mass-shell scheme (EOMS)

## Solution III: EOMS

#### Essence: The full integral can be separated into Infared Singular and Regular parts.



- Heavy baryon formalism (HB)
- □ Infrared Regularization (IR)
- Extended-on-mass-shell scheme (EOMS)

[Jenkins and Manohar, PLB255' 91]

[T.Becher and H.Leutwyler, Eur. Phys. J.C9' 99]

[T.Fuchs, J.Gegelia, G.Japaridze and S.Scherer, PRD68' 03]

